

MODELLING, ANALYSIS, AND OPTIMIZATION OF BPMN PROCESSES

GWEN SALAÜN

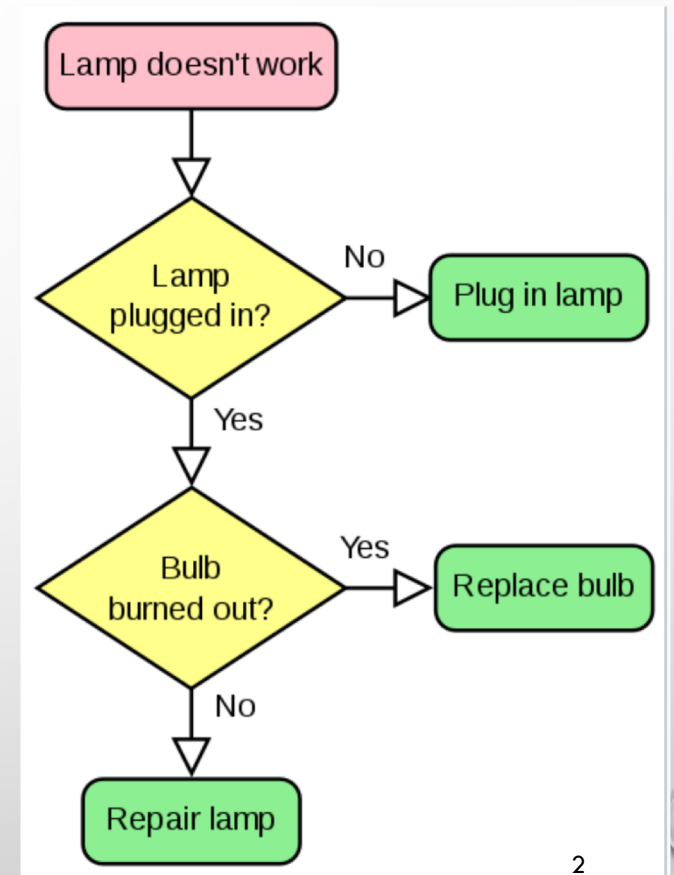


JOINT WORK WITH

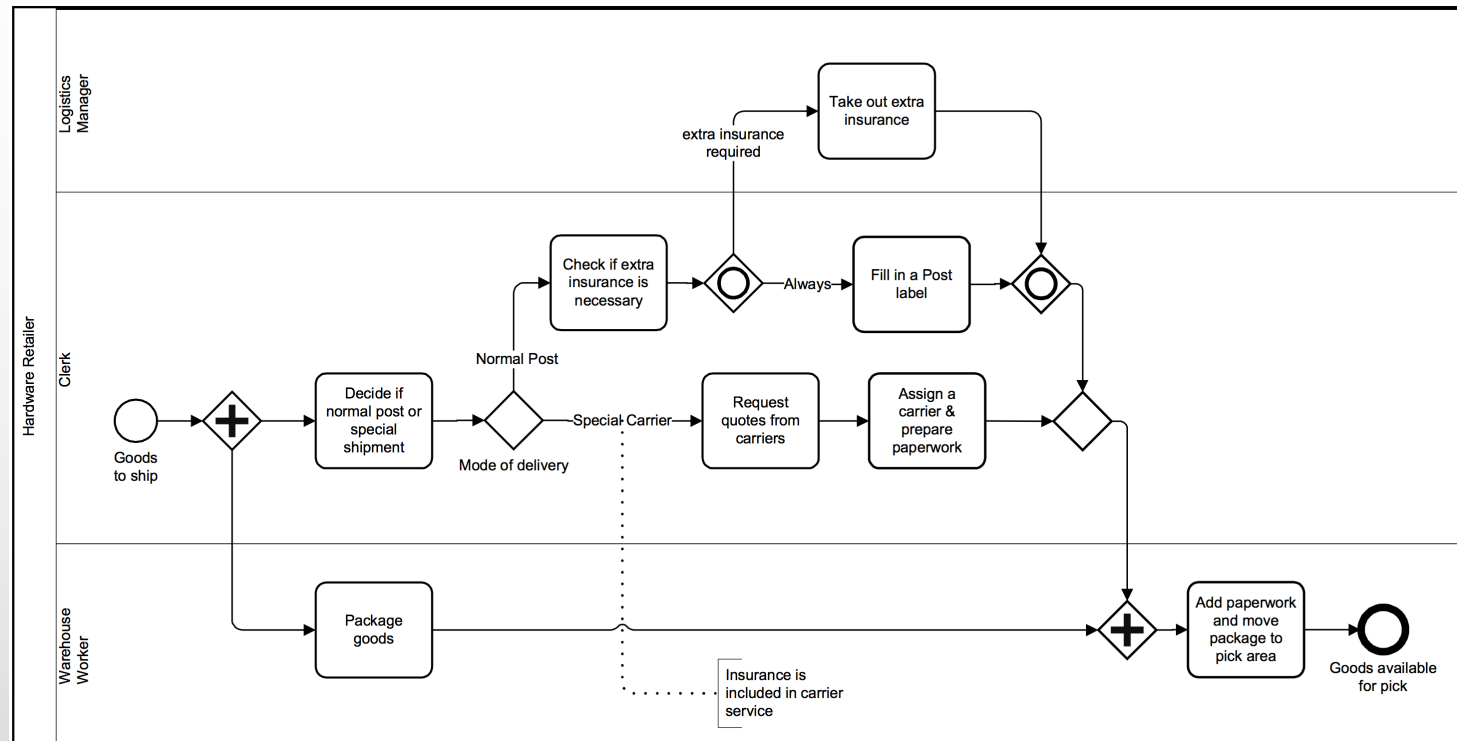
FRANCISCO DURÁN, YLIÈS FALCONE, CAMILO ROCHA AND AHANG ZUO

BUSINESS PROCESSES

“A **BUSINESS PROCESS** IS A COLLECTION OF RELATED, **STRUCTURED ACTIVITIES** OR **TASKS** BY PEOPLE OR EQUIPMENT IN WHICH A SPECIFIC SEQUENCE PRODUCES A **SERVICE** OR **PRODUCT** FOR A PARTICULAR **CUSTOMER**” (WIKIPEDIA)

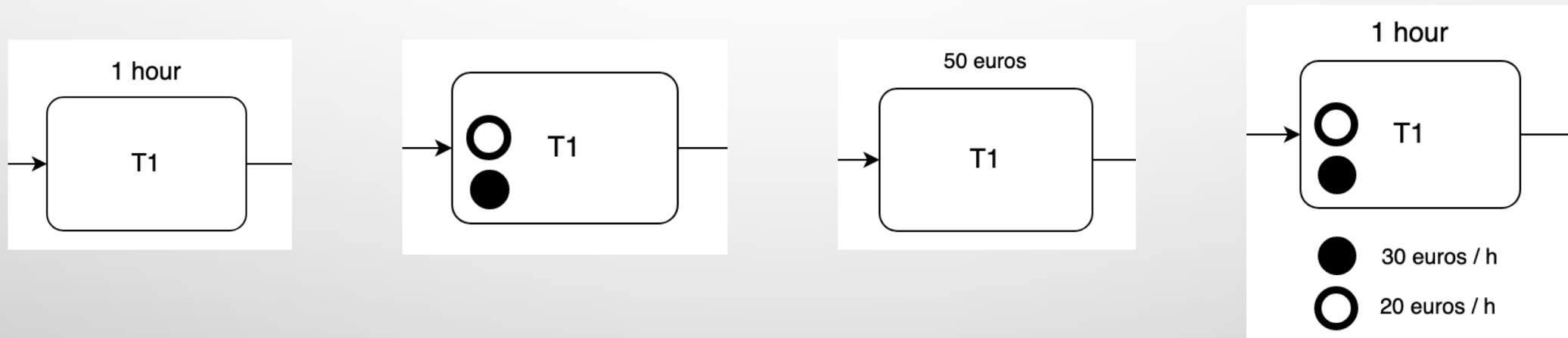


MODELLING PROCESSES WITH BPMN

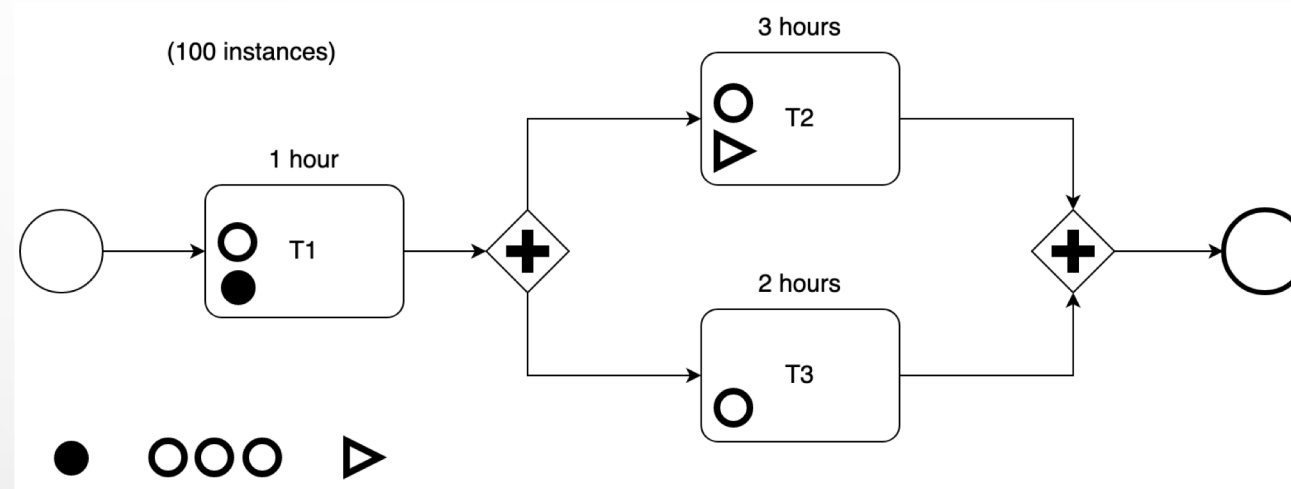


EXTENDED BPMN

BPMN EXTENDED WITH **QUANTITATIVE INFORMATION**: DURATIONS, RESOURCES, COSTS, POWER CONSUMPTION, CO2 EMISSION, ETC. (NOT MANDATORILY ALL AT THE SAME TIME)



MOTIVATING EXAMPLE

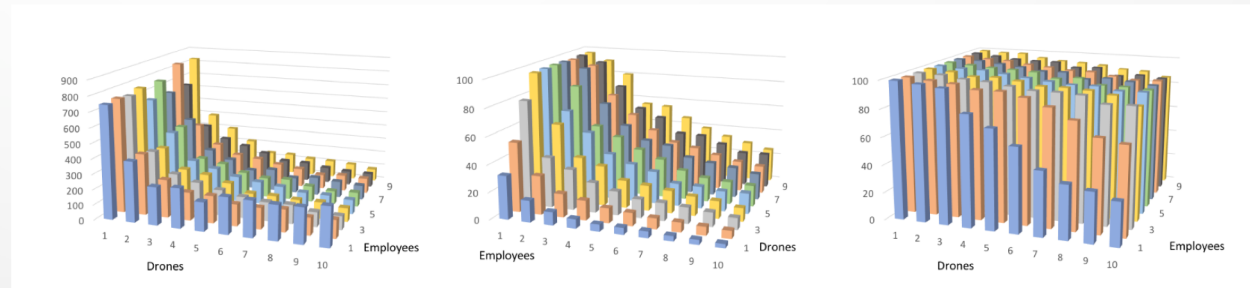


BPMN WITH TIME
AND RESOURCES

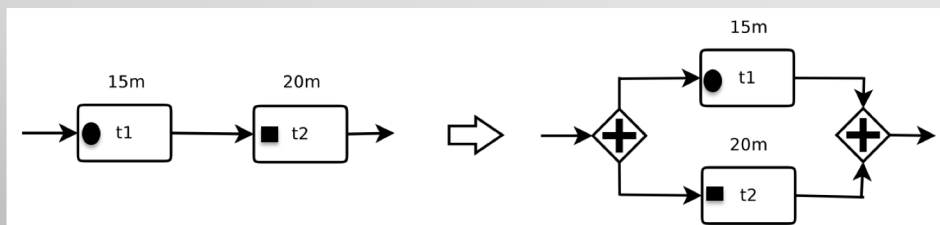
- HOW LONG DOES IT TAKE TO ONE INSTANCE TO COMPLETE IN AVERAGE ?
- HOW MUCH ARE EACH (TYPE OF) RESOURCE BUSY ?
- WHAT IS THE COST OF THIS EXECUTION ?
- WHAT IS THE OPTIMAL NUMBER OF RESOURCES FOR OPTIMIZING EXECUTION TIME AND/OR COST ?

CONTRIBUTIONS

- AN **EXTENSION OF BPMN** FOR MAKING EXPLICIT DESCRIPTION OF **TIME & RESOURCES**
- **AUTOMATED ANALYSIS** TECHNIQUES FOR COMPUTING **METRICS** ON RESOURCE USAGE, EXECUTION TIME AND COST



- PRESENTATION OF TWO POSSIBLE APPROACHES: **DESIGN TIME VS. RUNTIME ANALYSIS**
- ALTERNATIVE APPROACH FOR OPTIMIZING PROCESSES: **REFACTORIZING OF BPMN PROCESSES**



OUTLINE

1. BPMN WITH TIME AND RESOURCES
2. DESIGN TIME ANALYSIS
3. RUNTIME ANALYSIS
4. AUTOMATED REFACTORING
5. TOOL SUPPORT
6. CONCLUDING REMARKS

BPMN

BPMN 2.0 - Business Process Model and Notation <http://bpmb.de/poster>

Activities

Task
A Task is a unit of work, the job to be performed. It is the smallest unit of work in a process. It is represented by a rounded rectangle.

Sub-process
A Sub-process is a unit of work that is represented by a rounded rectangle with a thick border.

Event
An Event is a state in a process. It is represented by a circle with a thick border.

Call Activity
A Call Activity is a unit of work that is represented by a rounded rectangle with a thick border and a callout arrow.

Activity Markers
Markers are used to indicate the state of an activity. They are represented by small icons.

Task Types
Tasks are categorized into different types based on their execution. They are represented by different icons.

Conversations

Conversation Diagram
A Conversation Diagram is a type of process diagram that shows the interactions between different participants. It is represented by a rounded rectangle with a thick border.

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A Conversation Diagram is a type of process diagram that shows the interactions between different participants. It is represented by a rounded rectangle with a thick border.

Choreographies

Choreography Diagram
A Choreography Diagram is a type of process diagram that shows the interactions between different participants. It is represented by a rounded rectangle with a thick border.

Choreography Diagram
A Choreography Diagram is a type of process diagram that shows the interactions between different participants. It is represented by a rounded rectangle with a thick border.

Events

Event Type	Start	Intermediate	End
Start Event	Start		
Intermediate Event		Intermediate	
End Event			End

Gateways

Exclusive Gateway
An Exclusive Gateway is used to split a process into different paths. It is represented by a diamond with a thick border.

Parallel Gateway
A Parallel Gateway is used to split a process into different paths. It is represented by a diamond with a thick border.

Inclusive Gateway
An Inclusive Gateway is used to split a process into different paths. It is represented by a diamond with a thick border.

Complex Gateway
A Complex Gateway is used to split a process into different paths. It is represented by a diamond with a thick border.

Event-based Gateway
An Event-based Gateway is used to split a process into different paths. It is represented by a diamond with a thick border.

OR Gateway
An OR Gateway is used to split a process into different paths. It is represented by a diamond with a thick border.

AND Gateway
An AND Gateway is used to split a process into different paths. It is represented by a diamond with a thick border.

XOR Gateway
An XOR Gateway is used to split a process into different paths. It is represented by a diamond with a thick border.

AND-OR Gateway
An AND-OR Gateway is used to split a process into different paths. It is represented by a diamond with a thick border.

OR-AND Gateway
An OR-AND Gateway is used to split a process into different paths. It is represented by a diamond with a thick border.

AND-OR-AND Gateway
An AND-OR-AND Gateway is used to split a process into different paths. It is represented by a diamond with a thick border.

Collaboration Diagram

Collaboration Diagram
A Collaboration Diagram is a type of process diagram that shows the interactions between different participants. It is represented by a rounded rectangle with a thick border.

Collaboration Diagram
A Collaboration Diagram is a type of process diagram that shows the interactions between different participants. It is represented by a rounded rectangle with a thick border.

Swimlanes

Swimlanes
Swimlanes are used to group activities into different categories. They are represented by rounded rectangles with a thick border.

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Data

Data
Data is used to represent information in a process. It is represented by a rounded rectangle with a thick border.

Data
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CONTROL FLOWS AND GATEWAYS

→ sequence flow

○ → start state

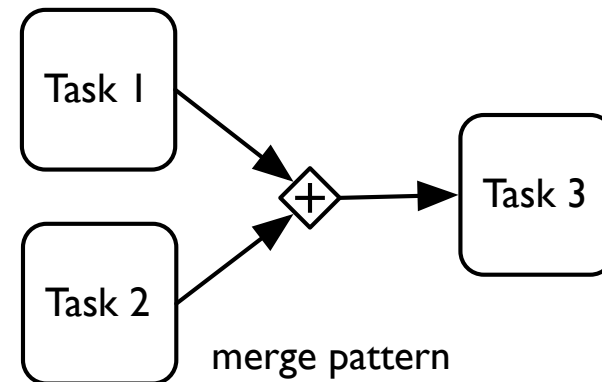
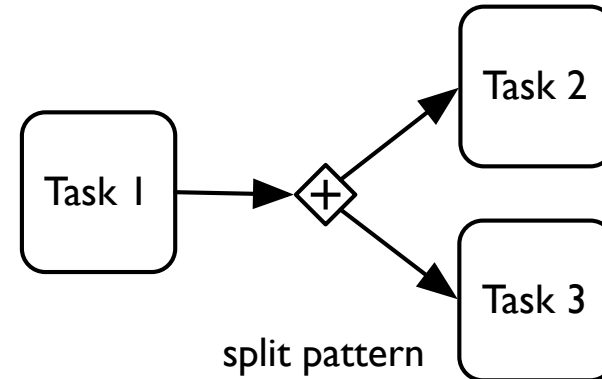
→ ⊙ end state

◇ or ◇~~X~~ exclusive gateway

◇⊙ inclusive gateway

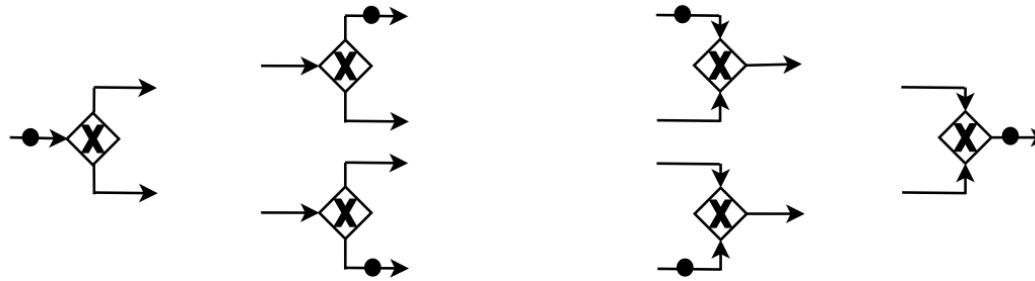
◇+ parallel gateway

◇⊙ or ◇⊙ event-based gateway



SEMANTICS

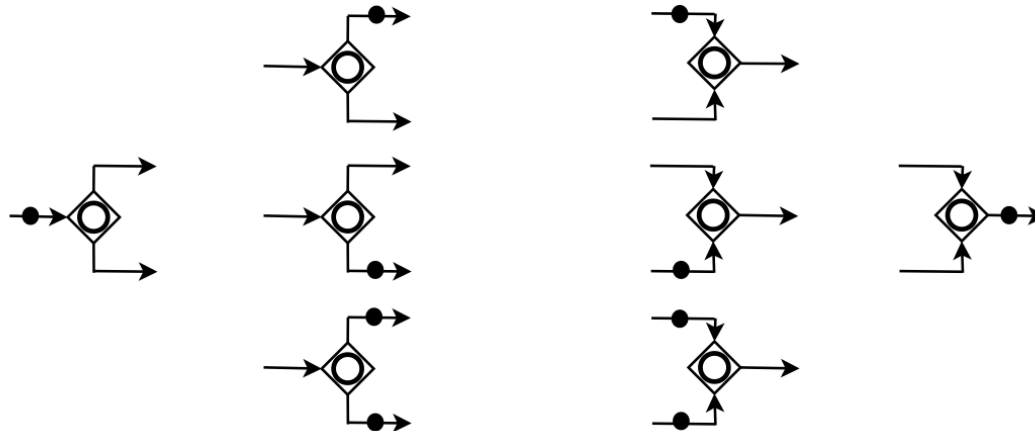
Exclusive gateway (similar for Event-based gateway): split (left) and merge (right)



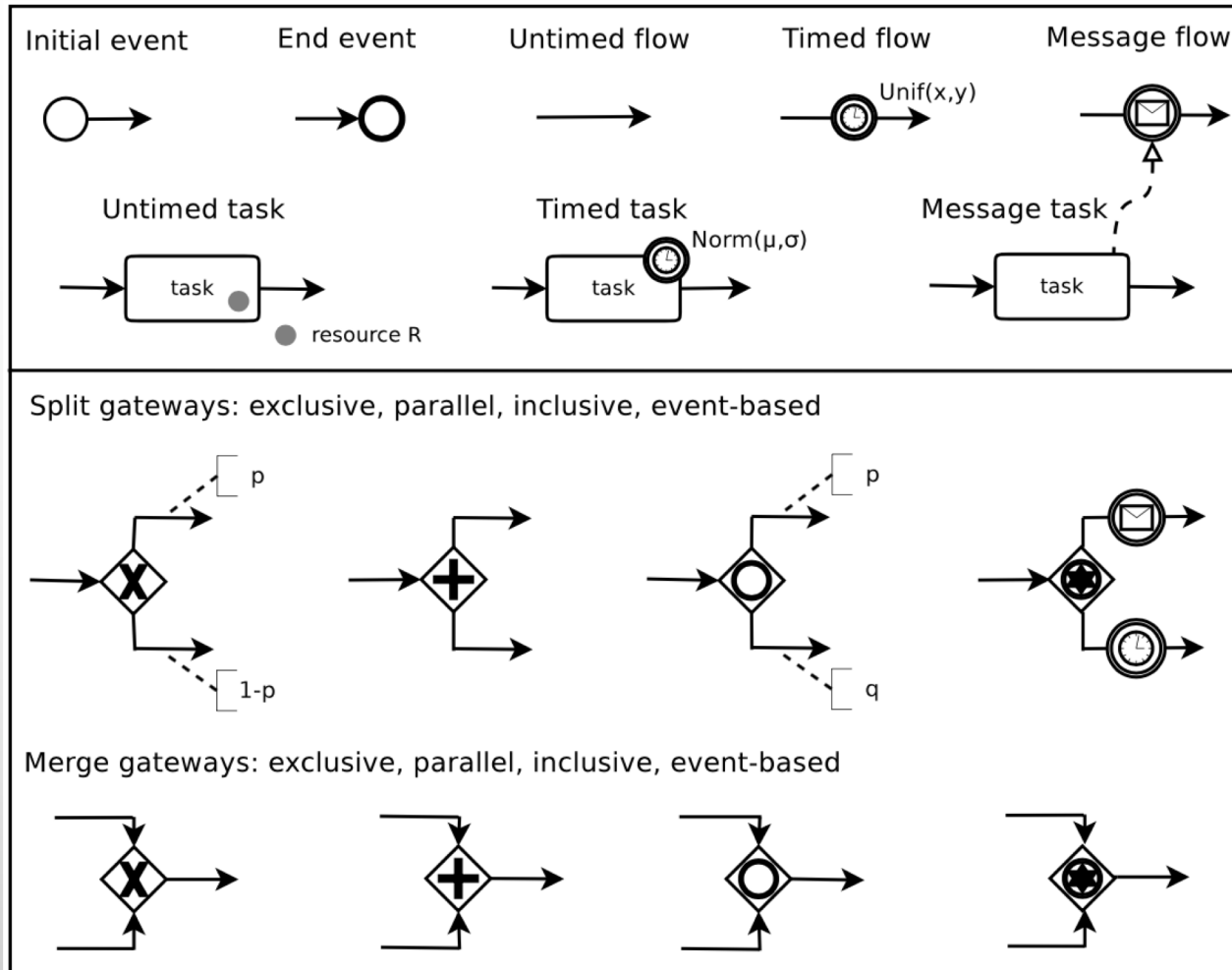
Parallel gateway : split (left) and merge (right)



Inclusive gateway : split (left) and merge (right)



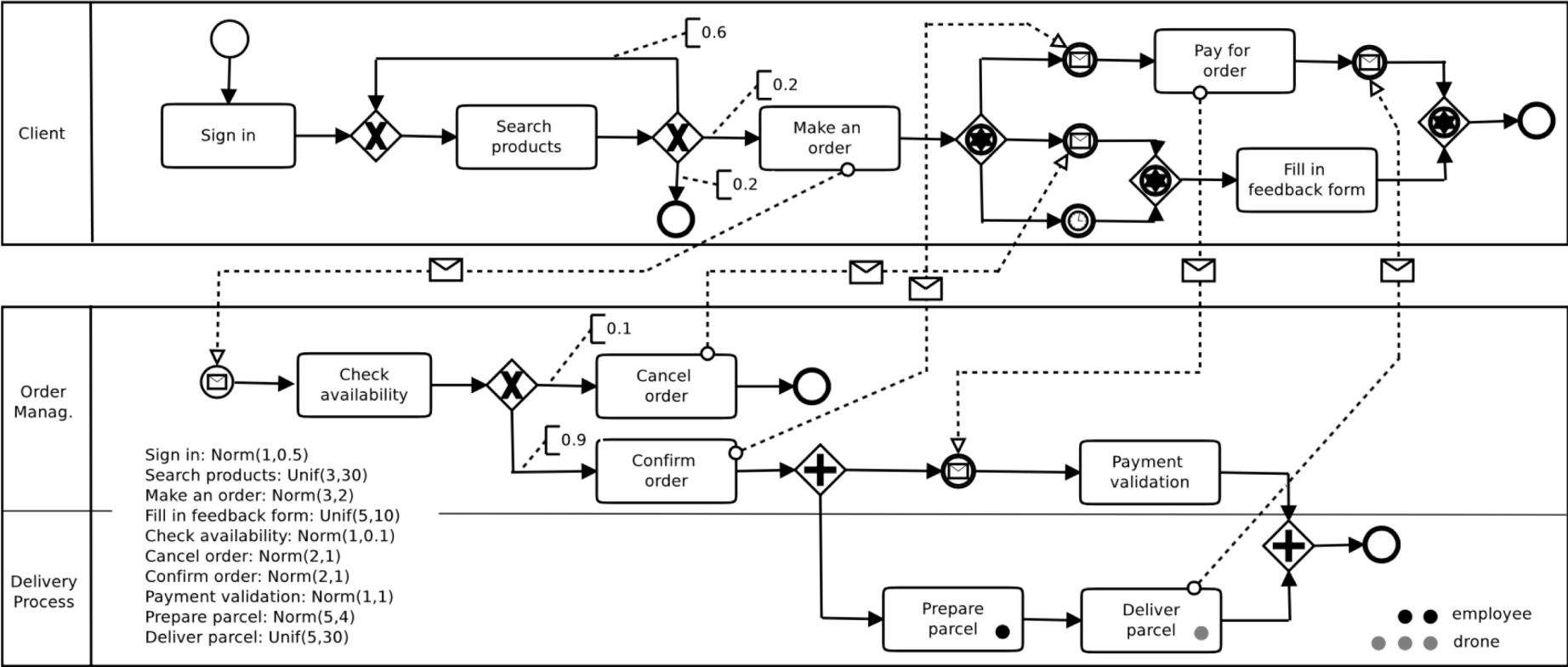
EXTENDED BPMN



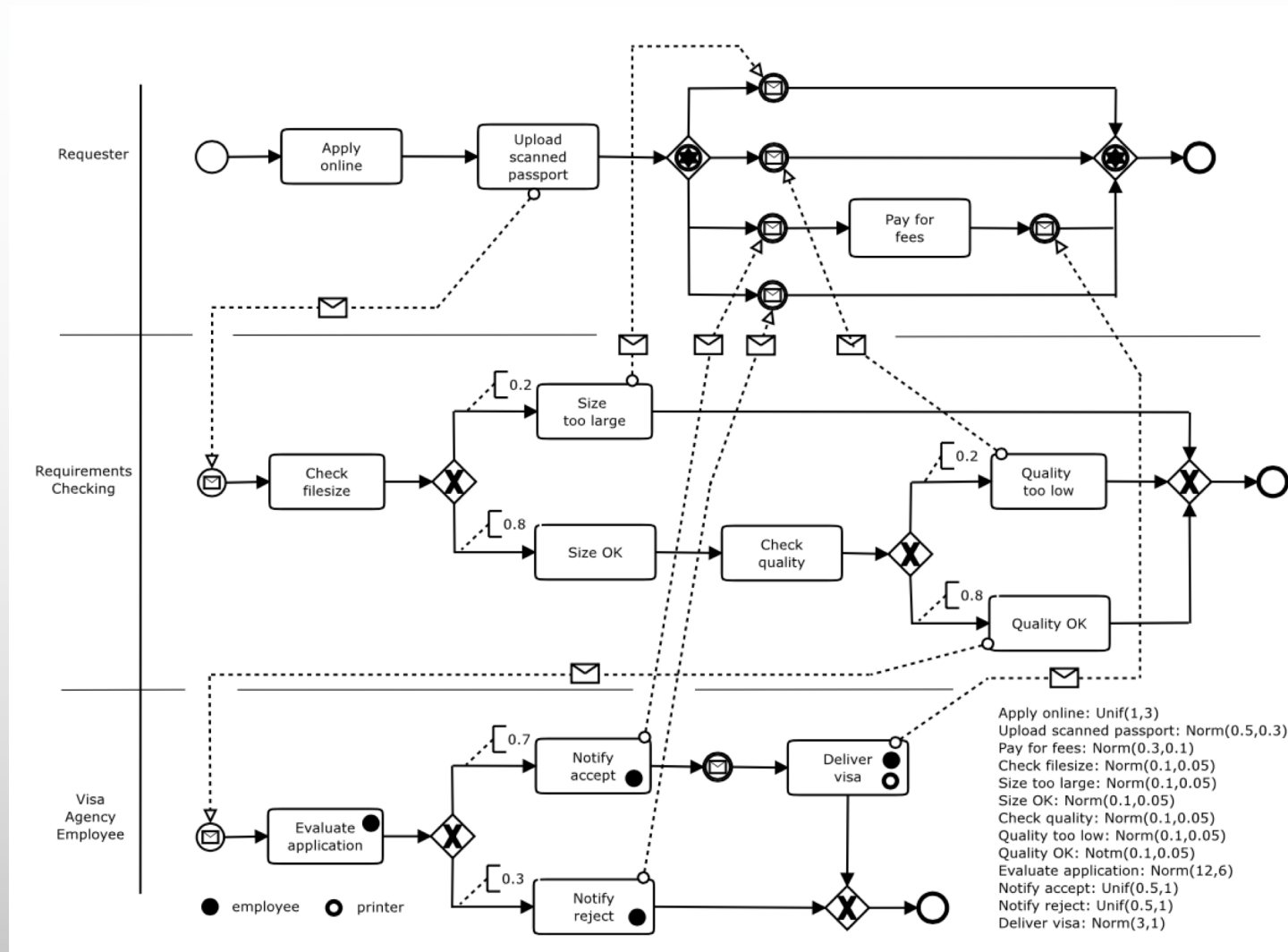
IN THIS WORK, WE SUPPORT

- ACTIVITY DIAGRAMS
- COLLABORATION DIAGRAMS

EXAMPLE: PRODUCT ORDER AND DELIVERY



EXAMPLE: VISA APPLICATION PROCESS

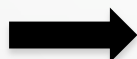
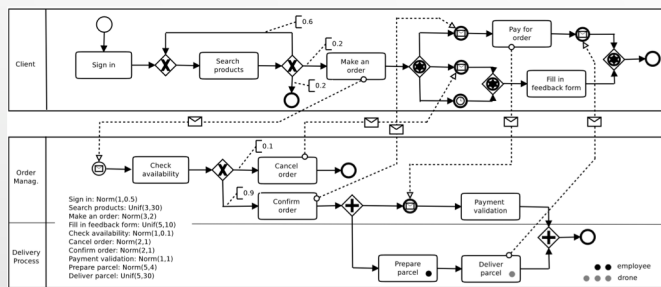


OUTLINE

1. BPMN WITH TIME AND RESOURCES
2. DESIGN TIME ANALYSIS
3. RUNTIME ANALYSIS
4. AUTOMATED REFACTORING
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6. CONCLUDING REMARKS

FORMAL MODEL

FORMAL SEMANTICS IS GIVEN TO THIS EXTENDED SUBSET OF BPMN BY ENCODING INTO REWRITING LOGIC



```
< pid : Process |
  nodes : (start(initial, cf1),
    merge(g1, exclusive, (cf2, cf5), cf3),
    split(g2, exclusive, cf4, ((cf5, 0.6) (cf6, 0.2) (cf7, 0.2))),
    split(g3, eventbased, cf8, (cf9, cf10, cf11)),
    task(t10, "Prepare parcel", mf7, df1, Norm(5.0, 4.0), employee, empty),
    task(t11, "Deliver parcel", df1, df2, Unif(5.0, 30.0), drone, parceldelivered),
    ...),
  flows : (flow(cf1, 0),
    flow(cf9, 0, message(orderconfirmed, "Order confirmed")),
    flow(cf10, 0, message(ordercanceled, "Order canceled")),
    flow(cf11, 0, timer(timeout, 60)),
    ...)
```

1.

```
< s : Simulation | tokens : ..., ----- scheduler
  gtime : ..., ----- global time
  resources : ..., ----- resource set
  events : ..., ----- event set
  process-execs : ....., ----- execution times
  sync-times : ..., ----- synchronization times
  task-times : ..., ----- task execution times
  ... >
```

2.

```
1 rl [initTask] :
2 < Pid : Process |
3 nodes : (task(NId, TaskName, FId1, FId2, SE, RIds, SEI), Nodes), Atts >
4 < Sid : Simulation |
5 tokens : (token(TId, FId1, 0) Tks),
6 task-tstamps : TTs, gtime : T, resources : Rs, Atts1 >
7 < Cid : Counter | counter : N >
8 => if allResourcesAvailable(RIds, Rs)
9 then < PID : Process |
10 nodes : (task(NId, TaskName, FId1, FId2, SE, RIds, SEI), Nodes), Atts >
11 < Sid : Simulation |
12 tokens : insert(Tks, token(TId, NId, time(eval(SE, N)))),
13 task-tstamps : if TTs[TId][NId] == undefined
14 then insert(TId, insert(NId, T, TTs[TId]), TTs)
15 else TTs
16 fi, ----- for loops, stamps get overwritten
17 gtime : T,
18 resources : grabResources&updateTime(RIds, Rs, time(eval(SE, N)), T), Atts1 >
19 < Cid : Counter | counter : int(eval(SE, N)) >
20 else ... ----- if necessary, the scheduler is updated
21 fi .
```

3.

THE MAUDE SPECIFICATION CONSISTS OF THREE PARTS:

1. **PROCESS SYNTAX** IS REPRESENTED AS AN OBJECT WITH A SET OF FLOWS AND A SET OF NODES AS ATTRIBUTE
2. THE **SIMULATION OBJECT** KEEPS INFORMATION ON THE EXECUTION OF THE PROCESS
3. **REWRITING RULES** REPRESENT HOW TOKENS EVOLVE THROUGH THE PROCESS AND EVENTS ARE FIRED

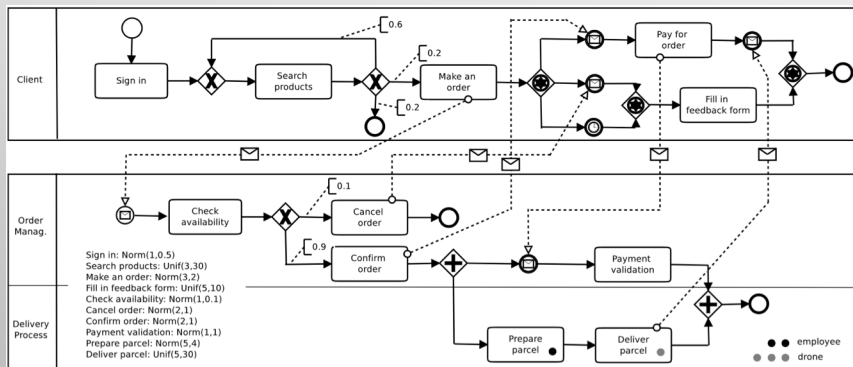
AUTOMATED ANALYSIS OF PROPERTIES

- **SIMULATION TECHNIQUES** TAKE AS INPUT: A PROCESS DESCRIPTION, A SPECIFICATION OF RESOURCES AND A WORKLOAD (NUMBER OF INSTANCES)
- **TIMING PROPERTIES:**
 - AVERAGE EXECUTION TIMES (AET) OF A PROCESS EXECUTION + SHORTEST / LONGEST EXECUTION
 - AVERAGE SYNCHRONIZATION TIME FOR MERGE GATEWAYS
- **RESOURCE-BASED PROPERTIES:**
 - THE GLOBAL TIME USAGE (GTU_R) OF ALL REPLICAS OF EACH RESOURCE R
 - THE GTU PER REPLICA OF RESOURCE R (GTU^1_R)
 - THE AVERAGE USAGE PERCENTAGE FOR EACH RESOURCE R OVER THE GLOBAL EXECUTION TIME (UP^1_R)
- **TOTAL COST**

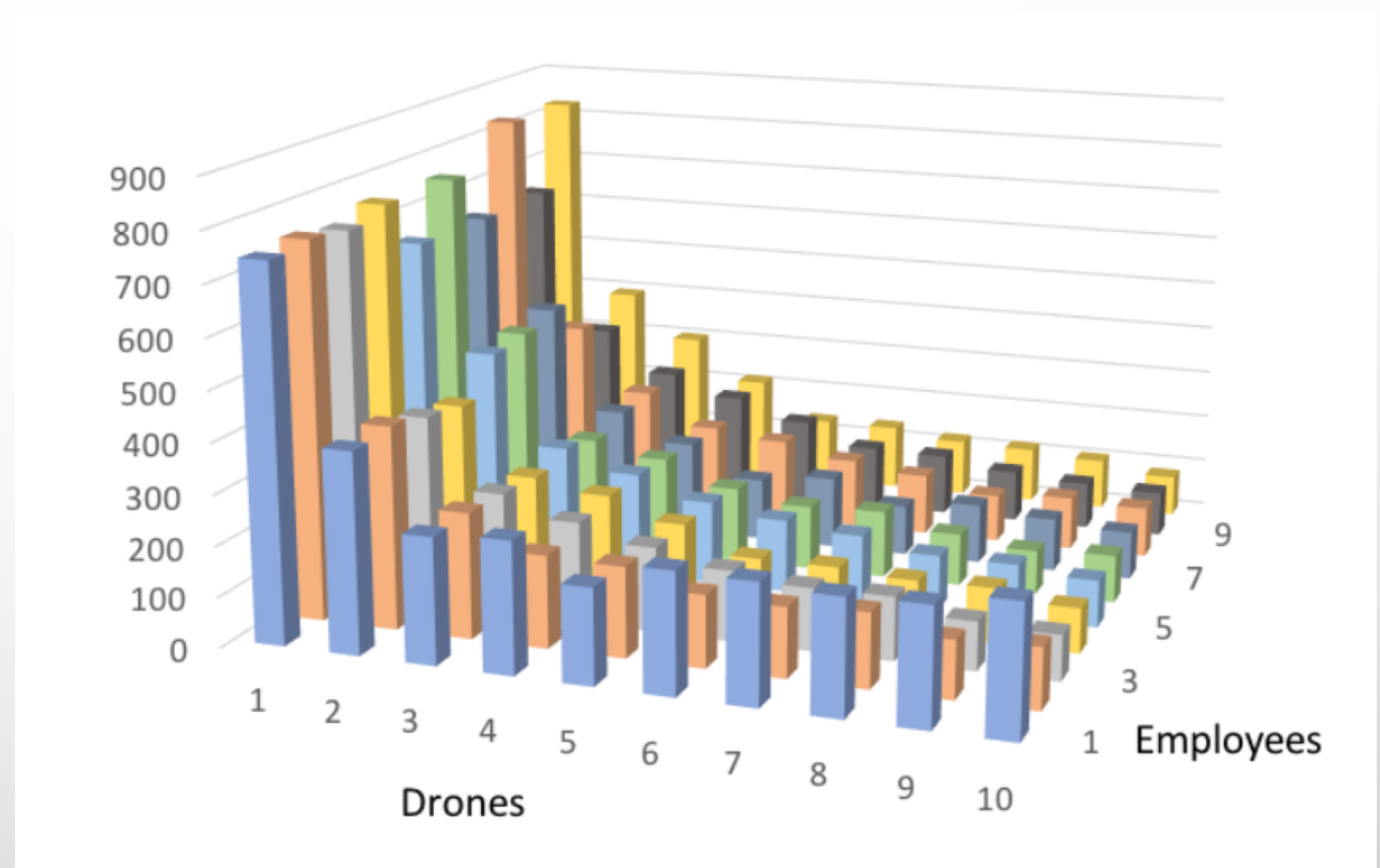
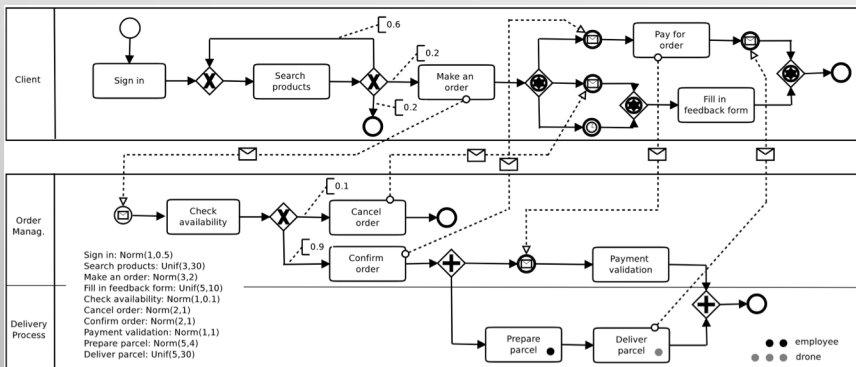
EXAMPLE: SIMULATION RESULTS

Numb. inst.	AET	Var	AST _{g8}	AST _{ee}	Total time	Resources						Analysis time
						GTU _e	GTU _e ¹	UP _e ¹	GTU _d	GTU _d ¹	UP _d ¹	
100	106	72	58	58	326	271	135	41	853	284	87	5s
200	185	134	71	139	670	514	257	38	1892	630	94	26s
400	284	173	98	237	1132	994	497	43	3270	1089	96	189s
800	506	294	145	459	2217	1867	933.6	42	6525	2171	98	1233s
1600	891	473	240	844	4187	3714	1857	44	12428	4142	98	7909s

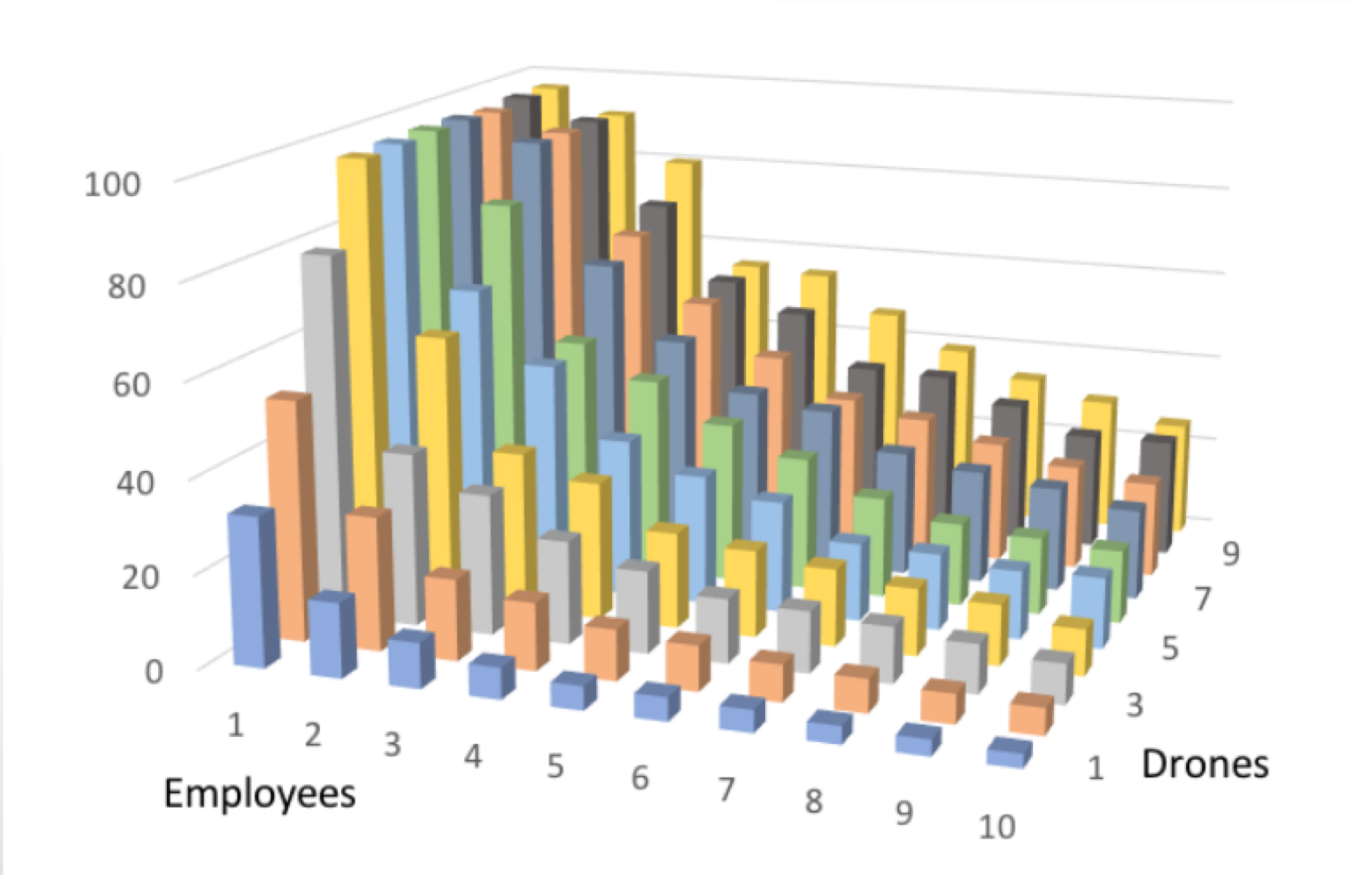
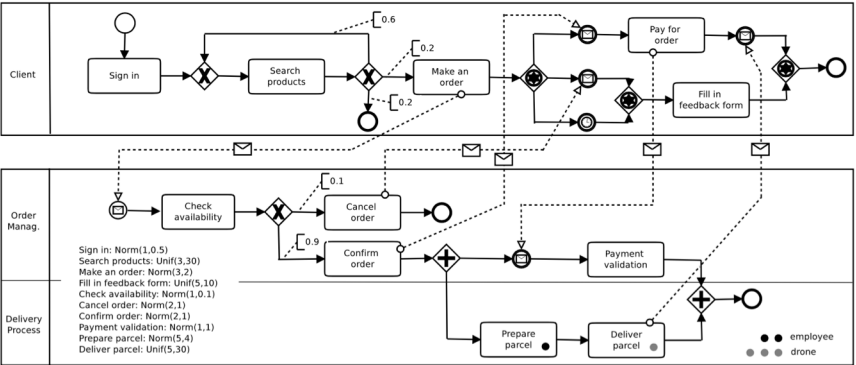
Table 1. Experimental results for the running example (2 employees, 3 drones)



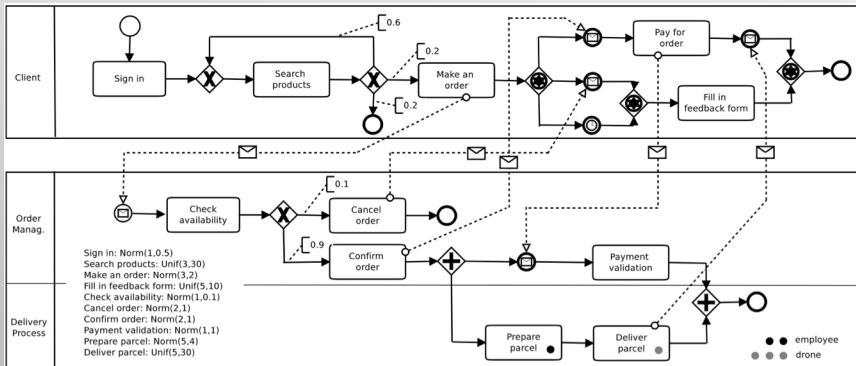
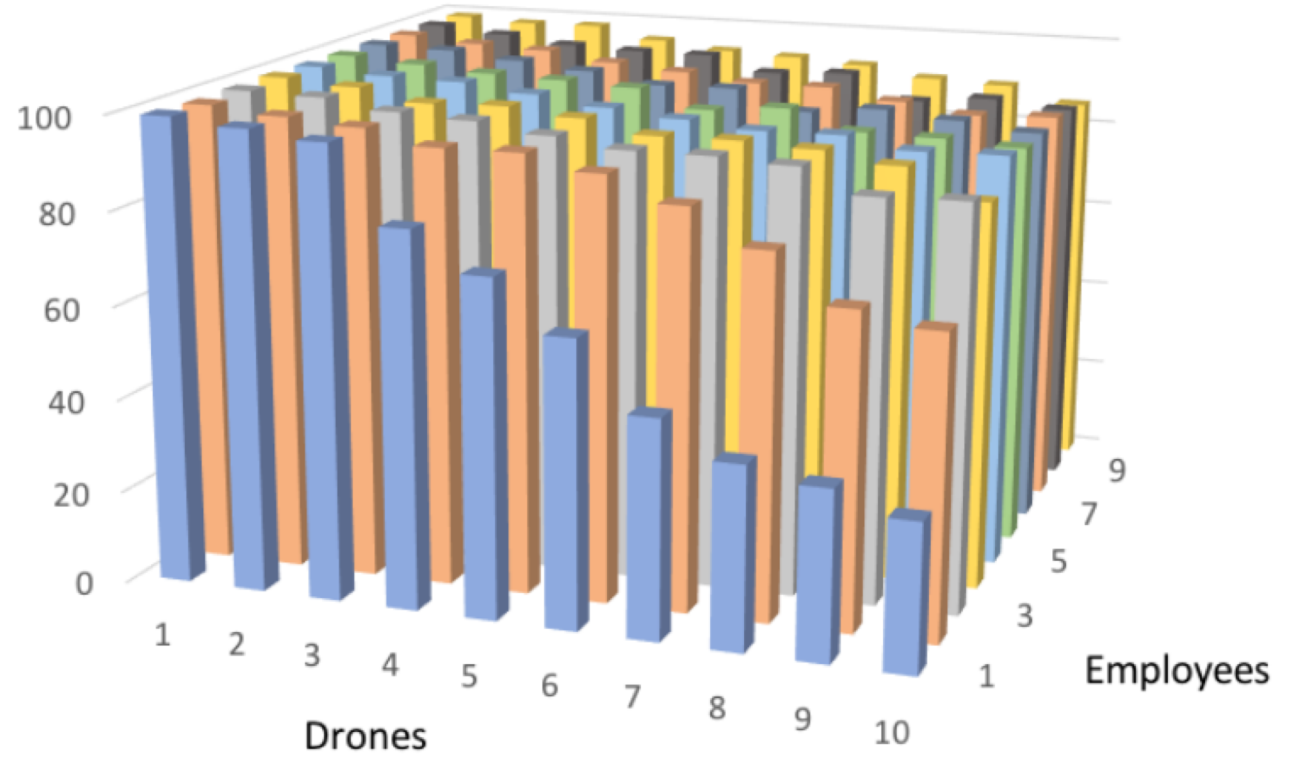
EXAMPLE: AVERAGE EXECUTION TIME



EXAMPLE: AVERAGE USAGE (EMPLOYEEE)



EXAMPLE: AVERAGE USAGE (DRONE)



OPTIMAL SOLUTIONS

COMPUTATION OF THE **OPTIMAL ALLOCATION** USING **MULTI-OBJECTIVE OPTIMIZATION** TECHNIQUES

$$\min_{x \in X} \sum_{i \in \{c,t\}} w_i f_i(x)$$

WHERE F_C AND F_T REPRESENT DRONE/EMPLOYEE COST AND AVERAGE EXECUTION TIME

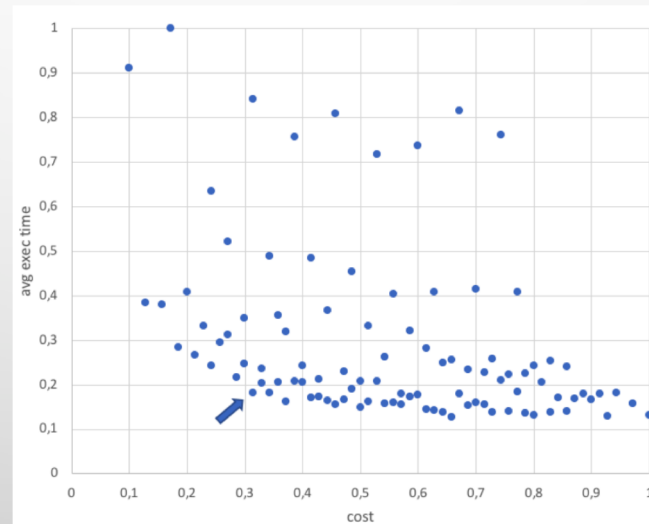
DRONE COST = 20€

EMPLOYEE COST = 50€

$w_c = 0.4$

$w_t = 0.6$

GOAL: MINIMIZE DELIVERY TIME

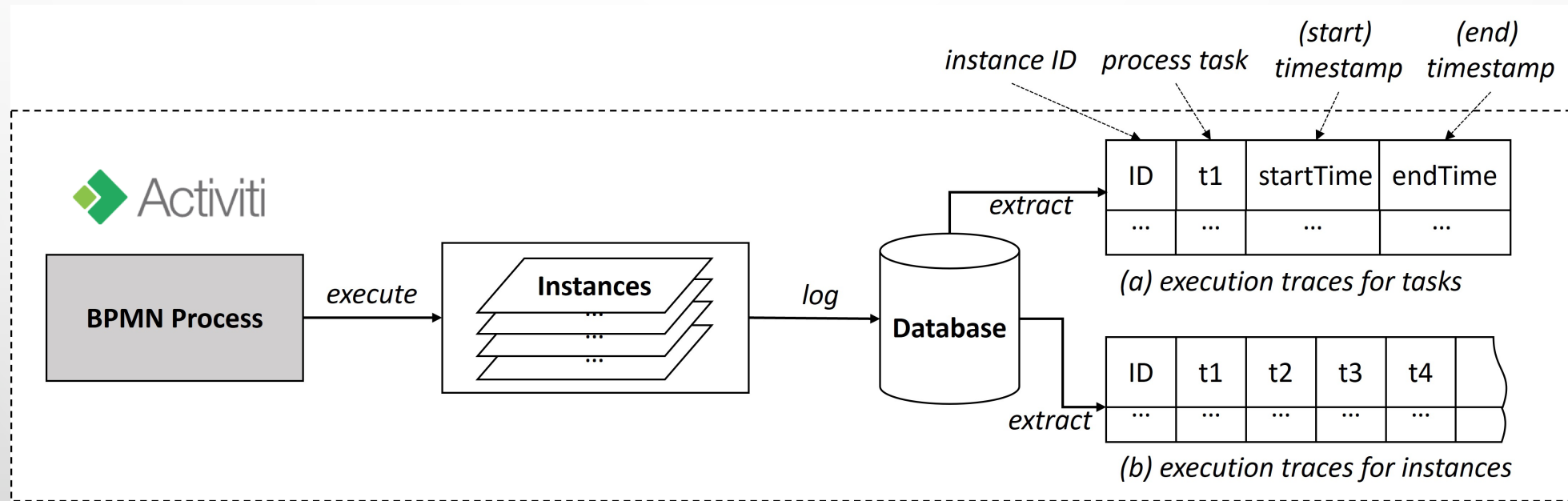


OPTIMAL SOLUTION:
6 DRONES AND 2 EMPLOYEES

OUTLINE

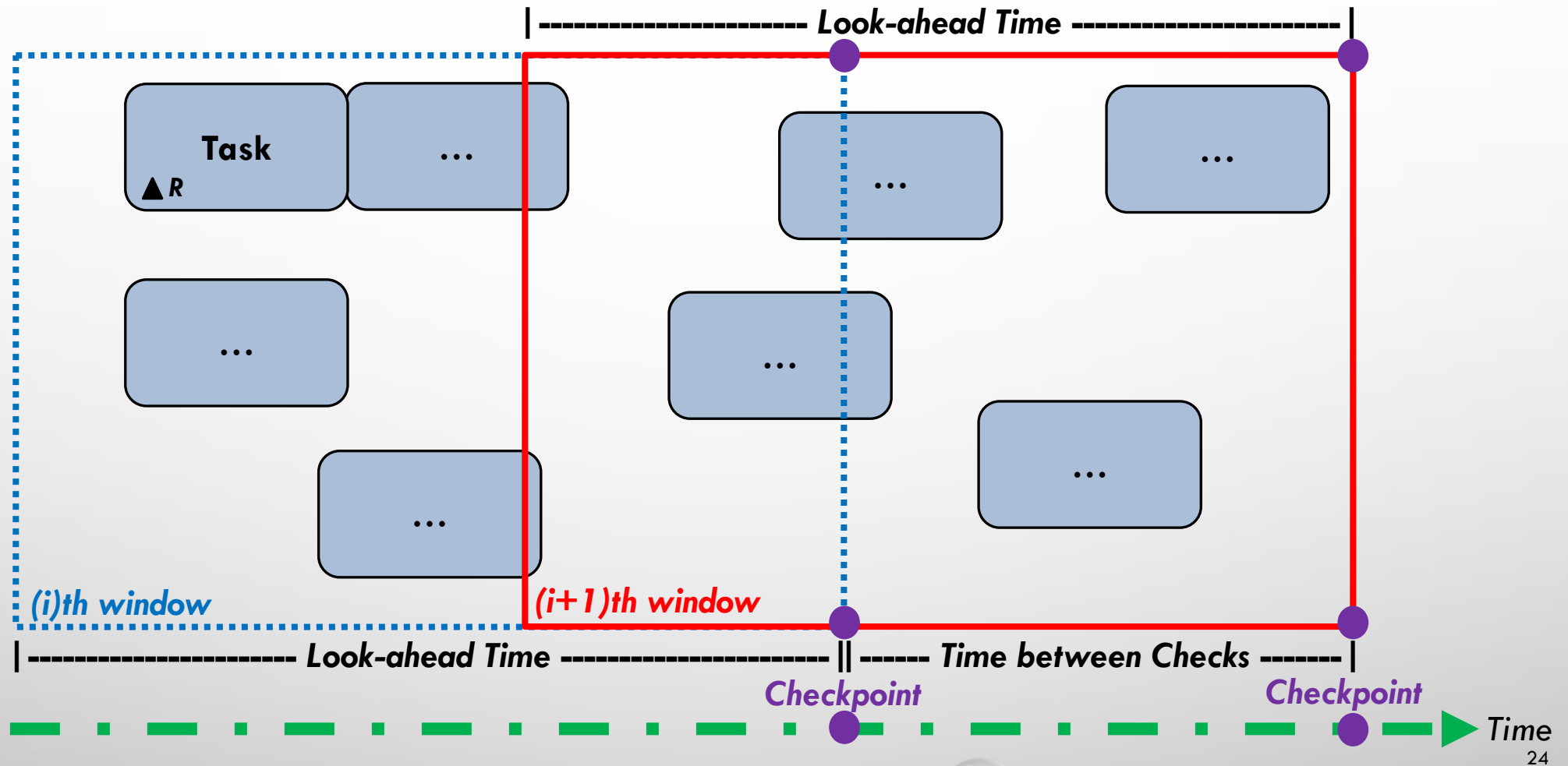
1. BPMN WITH TIME AND RESOURCES
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INSTRUMENTATION



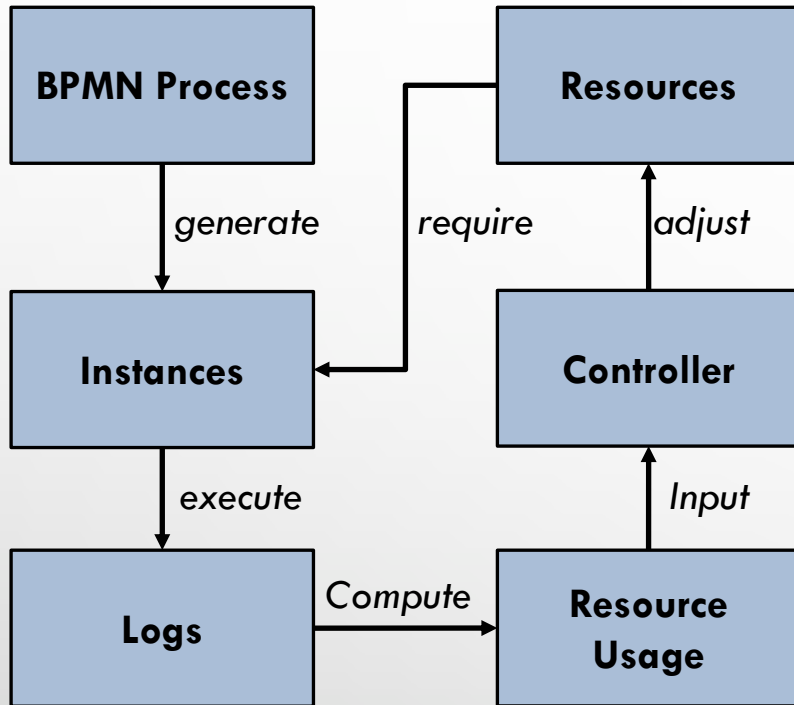
NO RESTRICTION ON
THE BPMN SYNTAX

COMPUTATION OF PROPERTIES



COMPUTE THE PROPERTIES FOR EACH WINDOW (E.G., RESOURCE USAGE OR AET)

DYNAMIC RESOURCE ALLOCATION



OVERVIEW OF THE APPROACH

$U(R)$: USAGE OF RESOURCE R .

$U_{current}(R)$: CURRENT USAGE OF RESOURCE R .

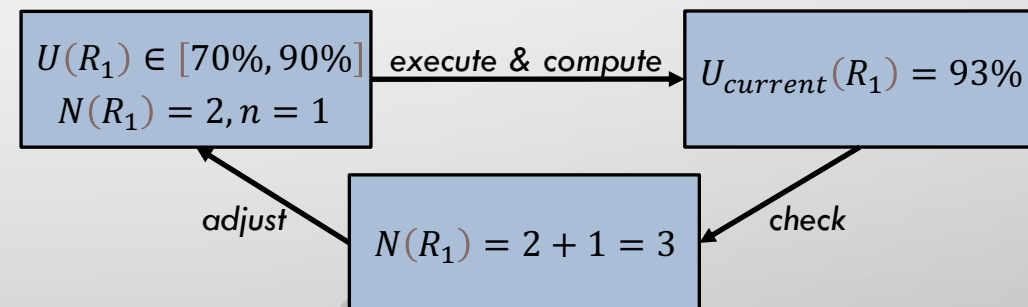
$N(R)$: NUMBER OF REPLICAS OF RESOURCE R , $N(R) > 0$.

EACH RESOURCE R IS DEFINED WITH A MINIMUM / MAXIMUM USAGE:

$$U(R) \in [minValue, maxValue]$$

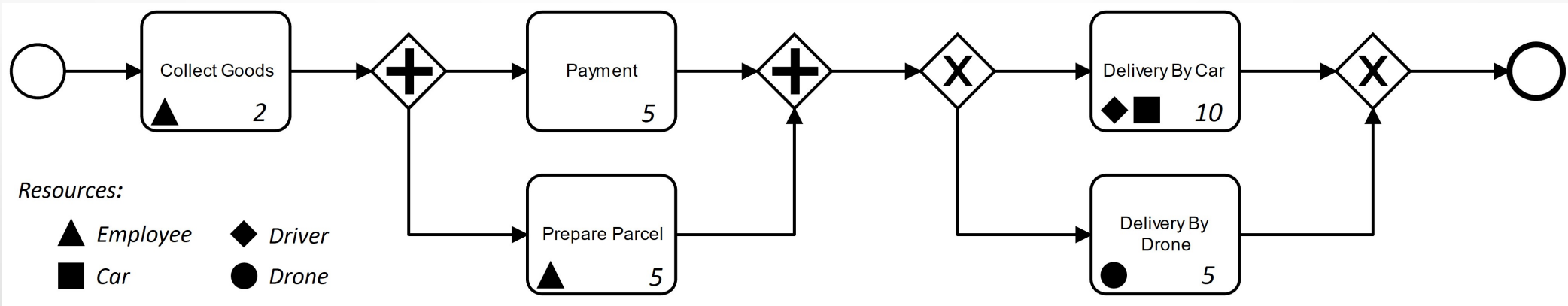
FOR EACH NEW WINDOW, WE CHECK:

- If $U_{current}(R) < minValue$, then $N(R) = N(R) - n$.
- If $U_{current}(R) > maxValue$, then $N(R) = N(R) + n$.
- OTHERWISE, NO OPERATION IS PERFORMED.

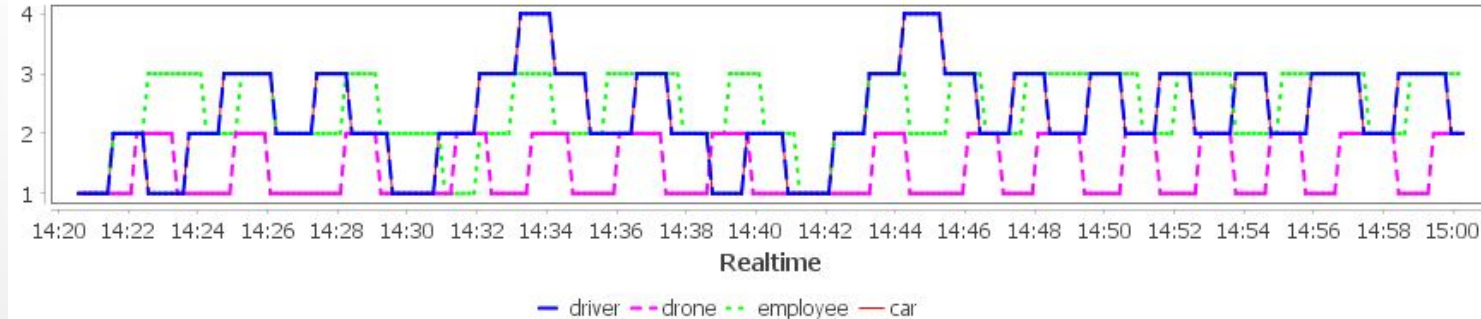


EXAMPLE OF THE APPROACH

EXAMPLE: GOODS DELIVERY PROCESS

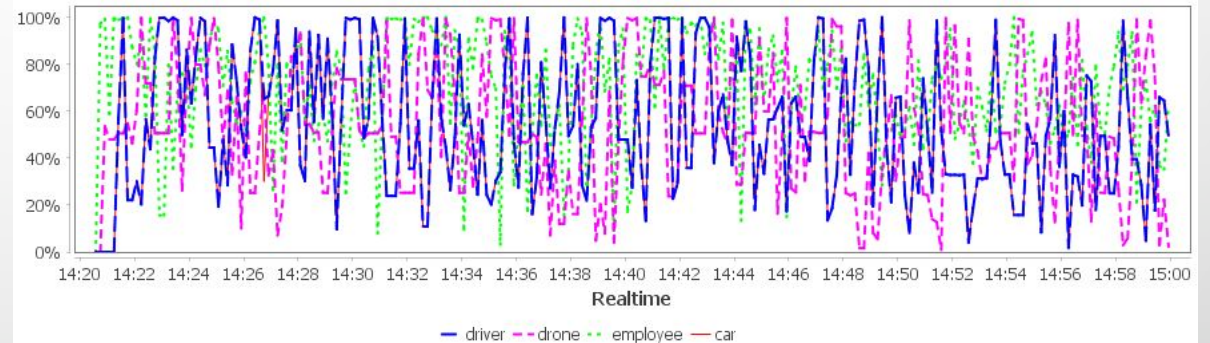


EXAMPLE: EXPERIMENTAL RESULTS

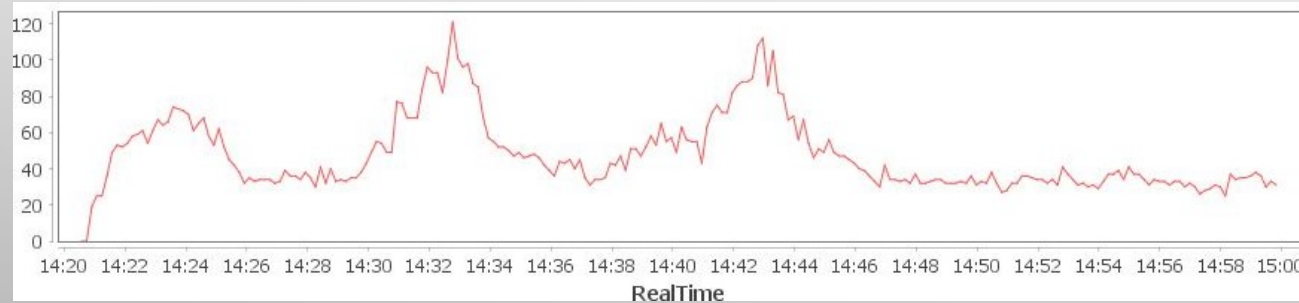


NUMBER OF REPLICAS

RESOURCE USAGE



AVERAGE EXECUTION TIME

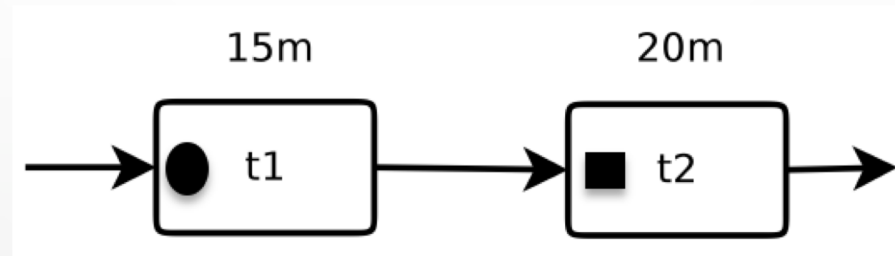


OUTLINE

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2. DESIGN TIME ANALYSIS
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4. **AUTOMATED REFACTORING**
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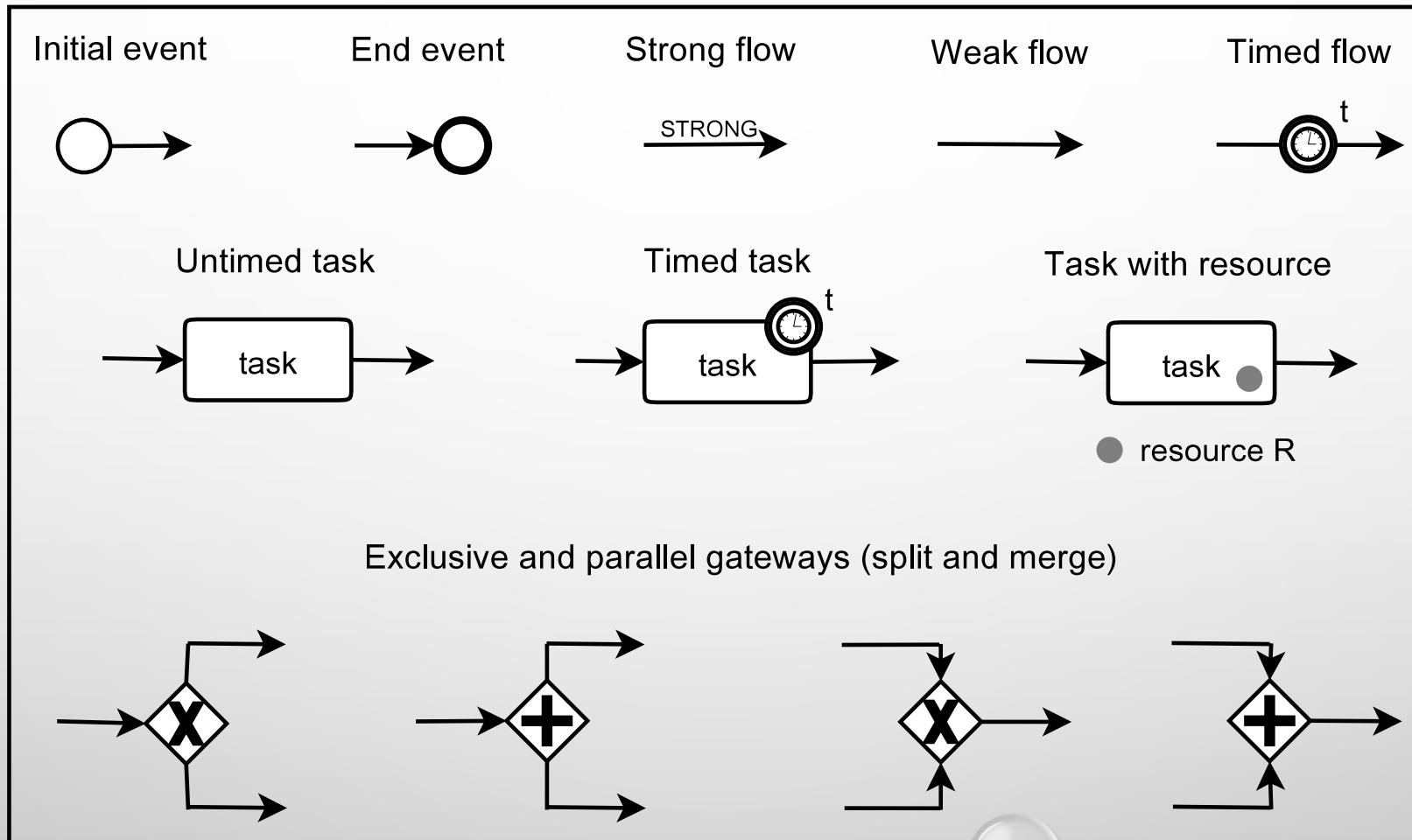
MOTIVATIONS

- ADJUSTING THE NUMBER OF RESOURCES DOES NOT ALWAYS INDUCE PROCESS OPTIMIZATION

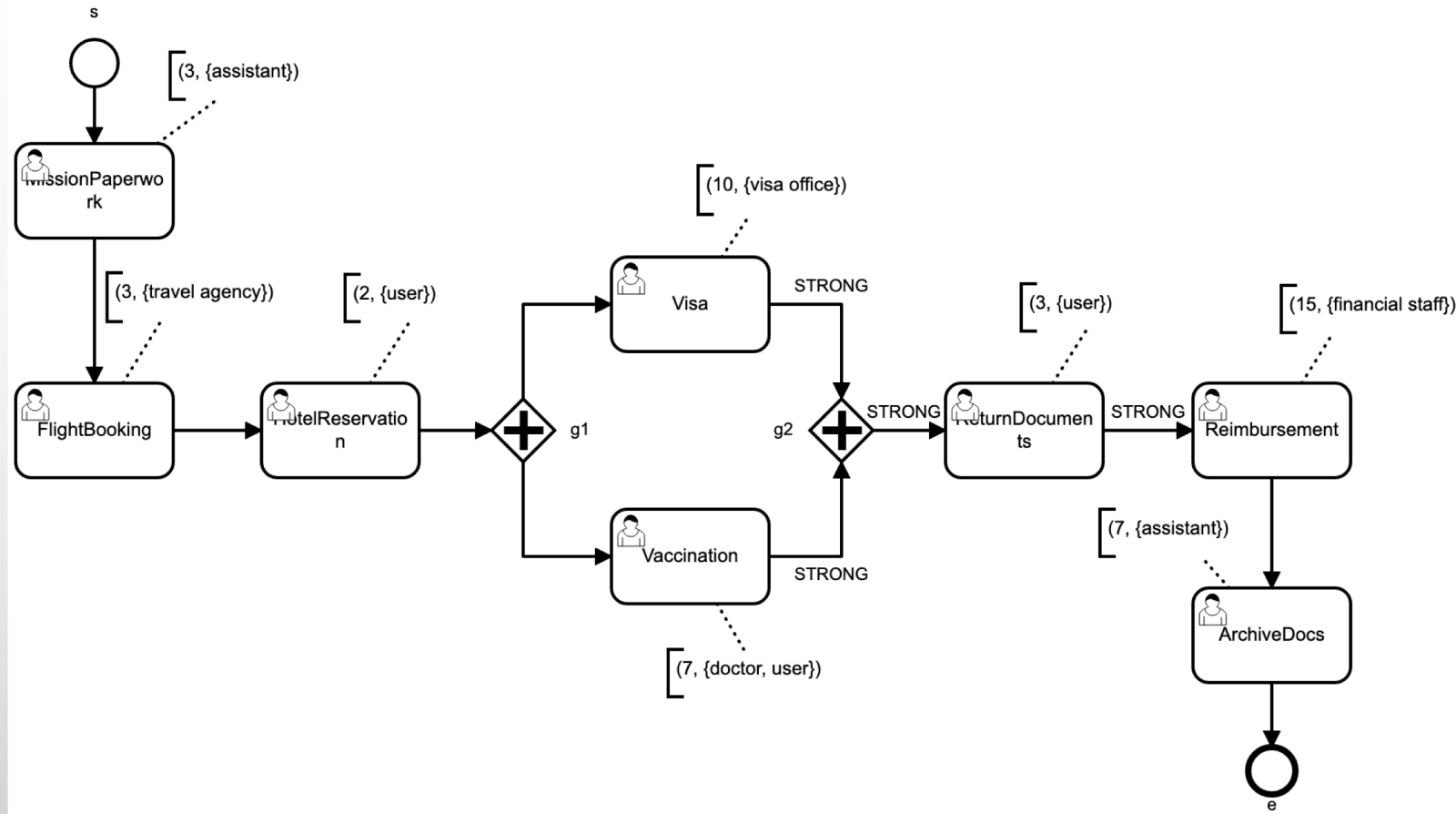


- SOLUTION: WE PROPOSE **REFACTORING TECHNIQUES** THAT **AUTOMATICALLY CHANGE THE STRUCTURE OF THE GIVEN INPUT PROCESS** WITH THE FINAL GOAL OF **REDUCING THE TOTAL EXECUTION TIME OF THE PROCESS**
- MAIN IDEA: **ADD PARALLELISM** AS OFTEN AS POSSIBLE

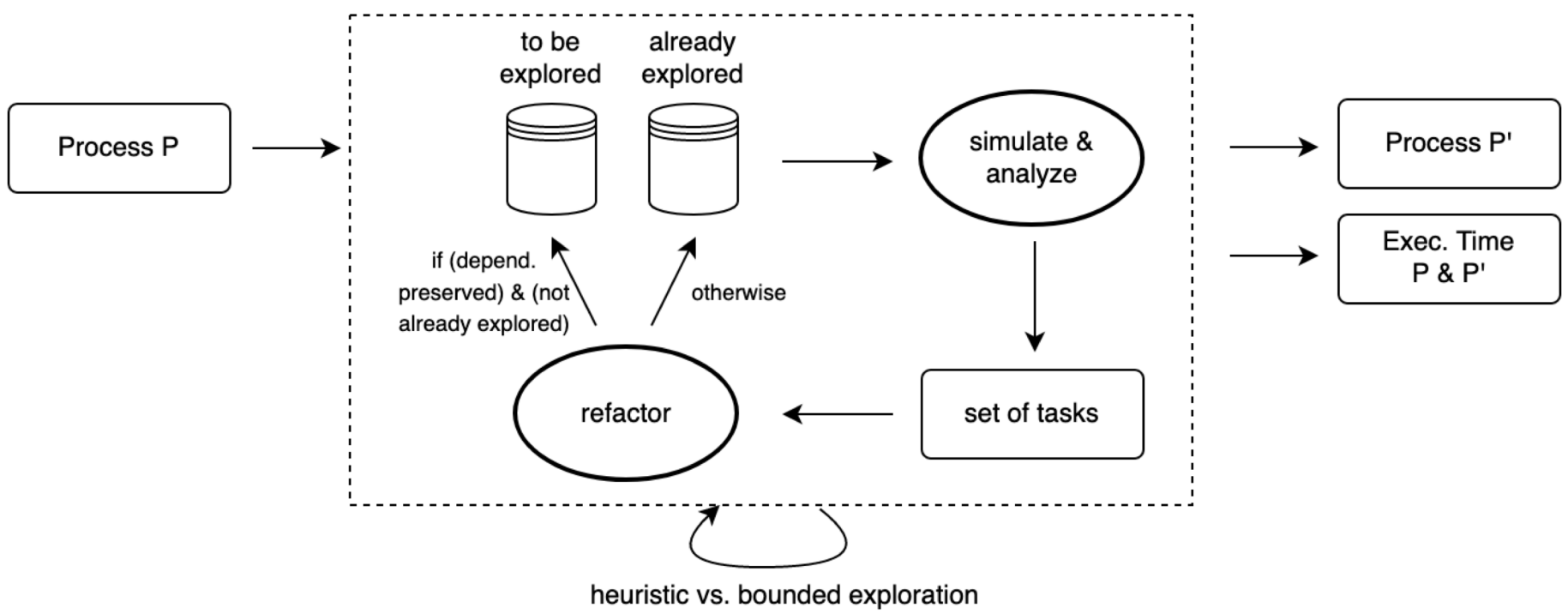
BPMN SYNTAX



TRIP ORGANIZATION PROCESS

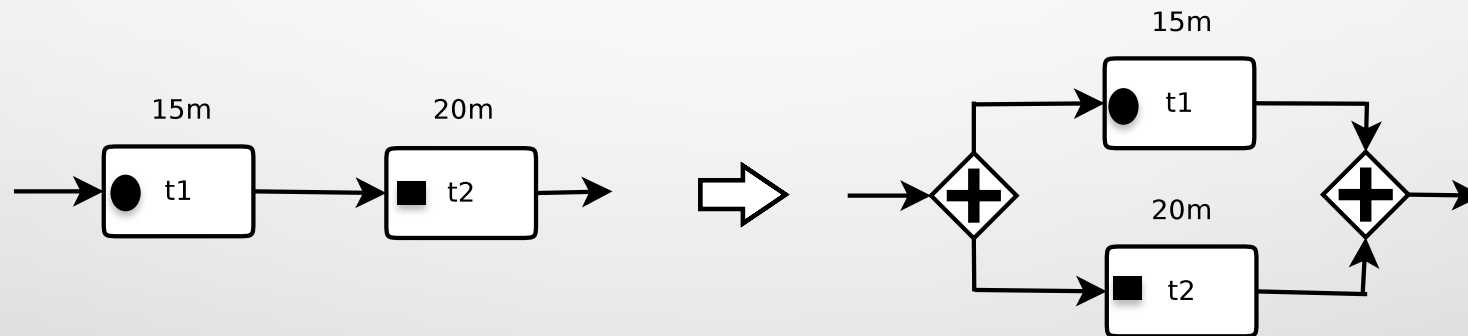


OVERVIEW



SIMULATION AND ANALYSIS

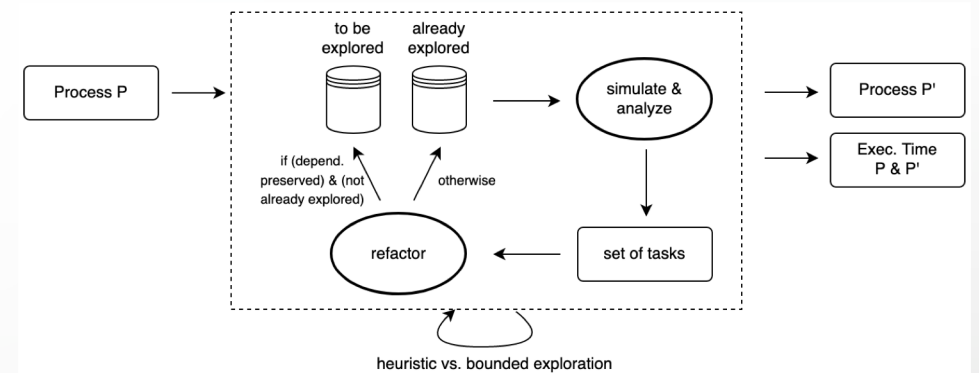
- **SIMULATION TECHNIQUES** EXECUTE THE PROCESS A **CERTAIN NUMBER OF TIMES** (PARAMETER) AND LOG DATA ABOUT THIS MULTIPLE EXECUTION
- ANALYSIS LOOKS FOR SPECIFIC MOMENTS DURING THE SIMULATION AT WHICH A TASK IS **STILL WAITING TO EXECUTE**, AND **ALL RESOURCES** REQUIRED FOR EXECUTING THIS TASK ARE **AVAILABLE**



- THIS MEANS THAT THIS SPECIFIC TASK COULD **EXECUTE EARLIER** IN THE PROCESS, AND THIS INFORMATION IS USED TO **CHANGE THE STRUCTURE** OF THE PROCESS

EXPLORATION OF RESULTS

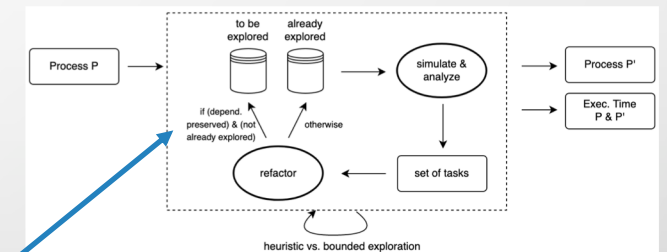
- THE WHOLE APPROACH APPLIES BY **SUCCESSIVE ITERATIONS**, AND STOPS WHEN THE QUEUE OF PROCESSES TO BE EXPLORED IS EMPTY



- THIS APPROACH MAY TAKE TIME, BECAUSE THERE MAY BE MANY PROCESSES TO BE EXPLORED, THEREFORE, SOME **STRATEGY** IS REQUIRED TO **GUIDE THE EXPLORATION OF NEW PROCESSES**
 - THE *FIRST STRATEGY* APPLIES REFACTORING FOR THE **TASK CLOSER TO THE INITIAL EVENT** IN THE PROCESS BY TRYING TO MOVE FIRST THE TASK CLOSER TO ITS FINAL POSITION
 - THE *SECOND STRATEGY* IS AN **EXHAUSTIVE EXPLORATION** OF ALL PROCESSES TO BE EXPLORED **UP TO A CERTAIN BOUND**

REFACTORING PATTERNS

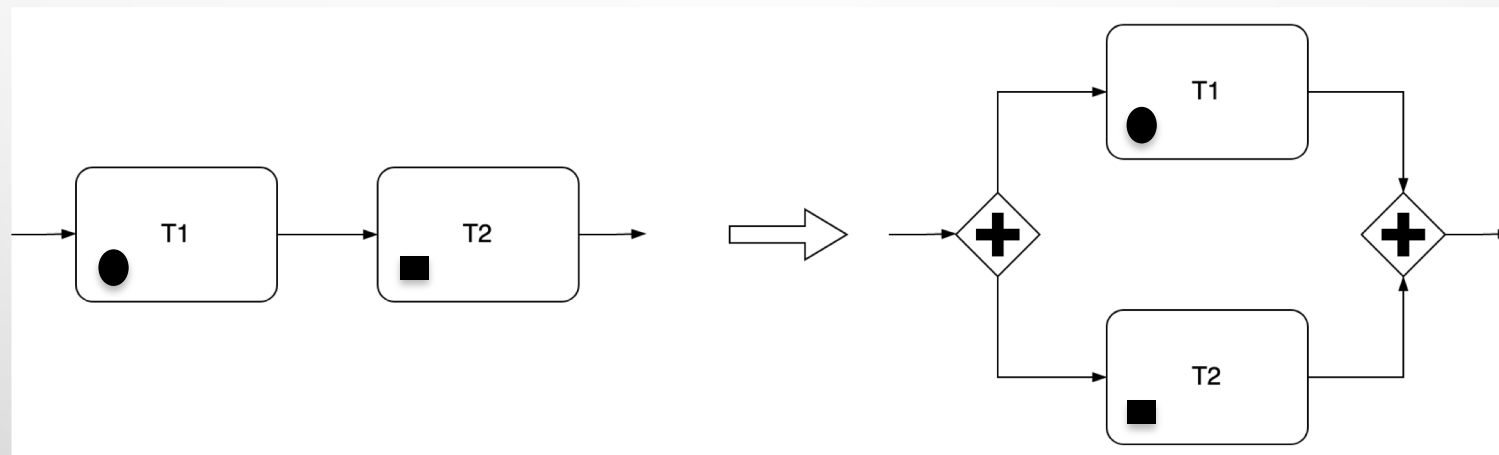
- GIVEN AS INPUT A PROCESS AND A TASK THAT HAS TO BE MOVED EARLIER IN THE PROCESS, REFACTORING RETURNS A **NEW PROCESS** AS OUTPUT
- THE REFACTORING PATTERN TO BE APPLIED DEPENDS ON WHAT **TYPE OF NODE** PRECEDES THE TASK TO BE MOVED BACKWARDS, WHICH CAN BE:
 - ANOTHER **TASK**
 - A **MERGE GATEWAY** (PARALLEL / EXCLUSIVE)
 - A **SPLIT GATEWAY** (PARALLEL / EXCLUSIVE)



- THIS REFACTORING STEP FOCUSES ON THE PROCESS STRUCTURE AND ON THE USAGE OF RESOURCES BY TASKS, BUT DOES NOT TAKE INTO ACCOUNT **STRONG FLOWS**

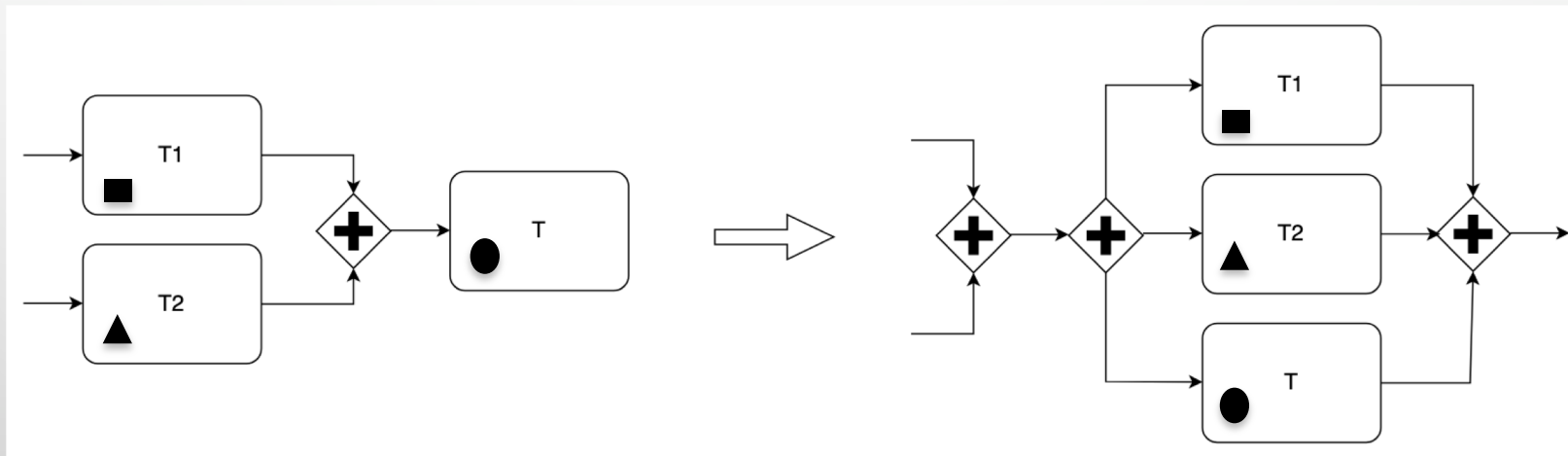
REFACTORING PATTERNS: TASK

IF THE TASK IS PRECEDED BY ANOTHER TASK, AND IF THEY **DO NOT SHARE ANY RESOURCES**, WE TRANSFORM THE PROCESS TO EXECUTE THESE TWO TASKS WITHIN A COMMON PARALLEL GATEWAY



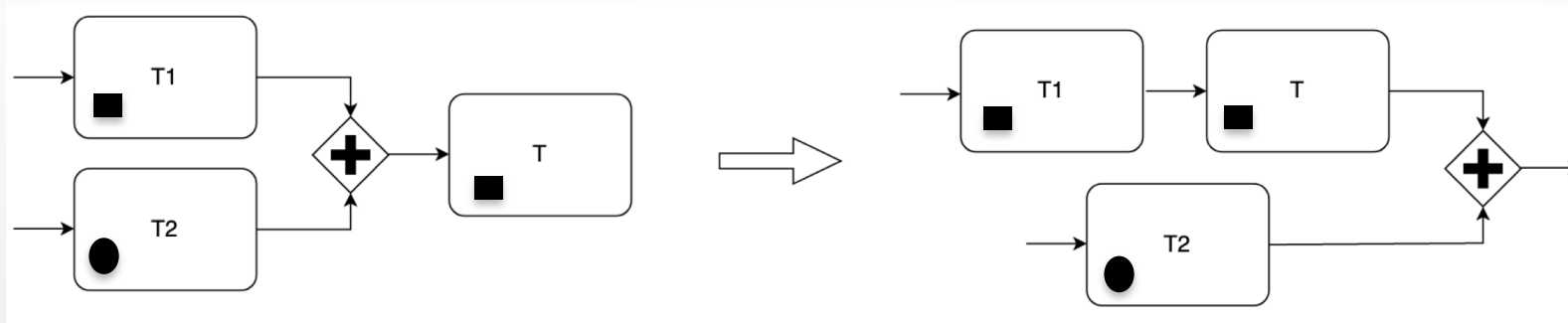
REF. PATTERNS: MERGE PARALLEL GATEWAY (1 / 2)

IF THE TASK 'T' IS PRECEDED BY A MERGE PARALLEL GATEWAY, IF THAT MERGE IS PRECEDED BY A SET OF TASKS, AND NONE OF THESE TASKS SHARE RESOURCES WITH 'T', THEN **ALL TASKS** ARE GATHERED **IN PARALLEL** BEFORE THE MERGE GATEWAY

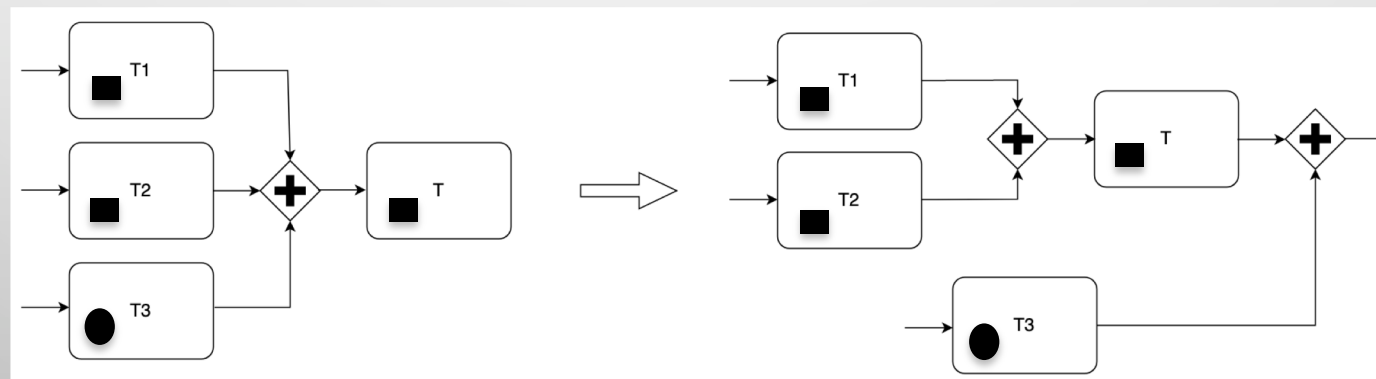


REF. PATTERNS: MERGE PARALLEL GATEWAY (2/2)

- MERGE PARALLEL GATEWAY WITH PRECEDING TASKS (SHARED RESOURCES WITH ONE TASK)

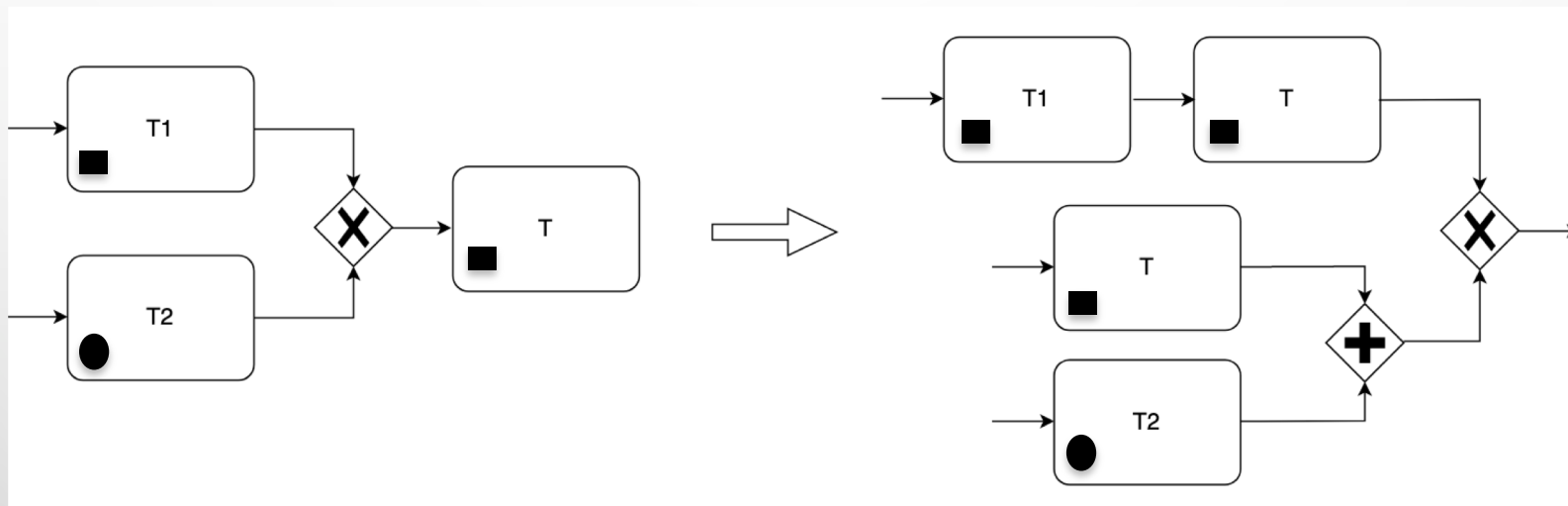


- MERGE PARALLEL GATEWAY WITH PRECEDING TASKS (SHARED RESOURCES WITH SEVERAL TASKS)



REF. PATTERNS: MERGE EXCLUSIVE GATEWAY

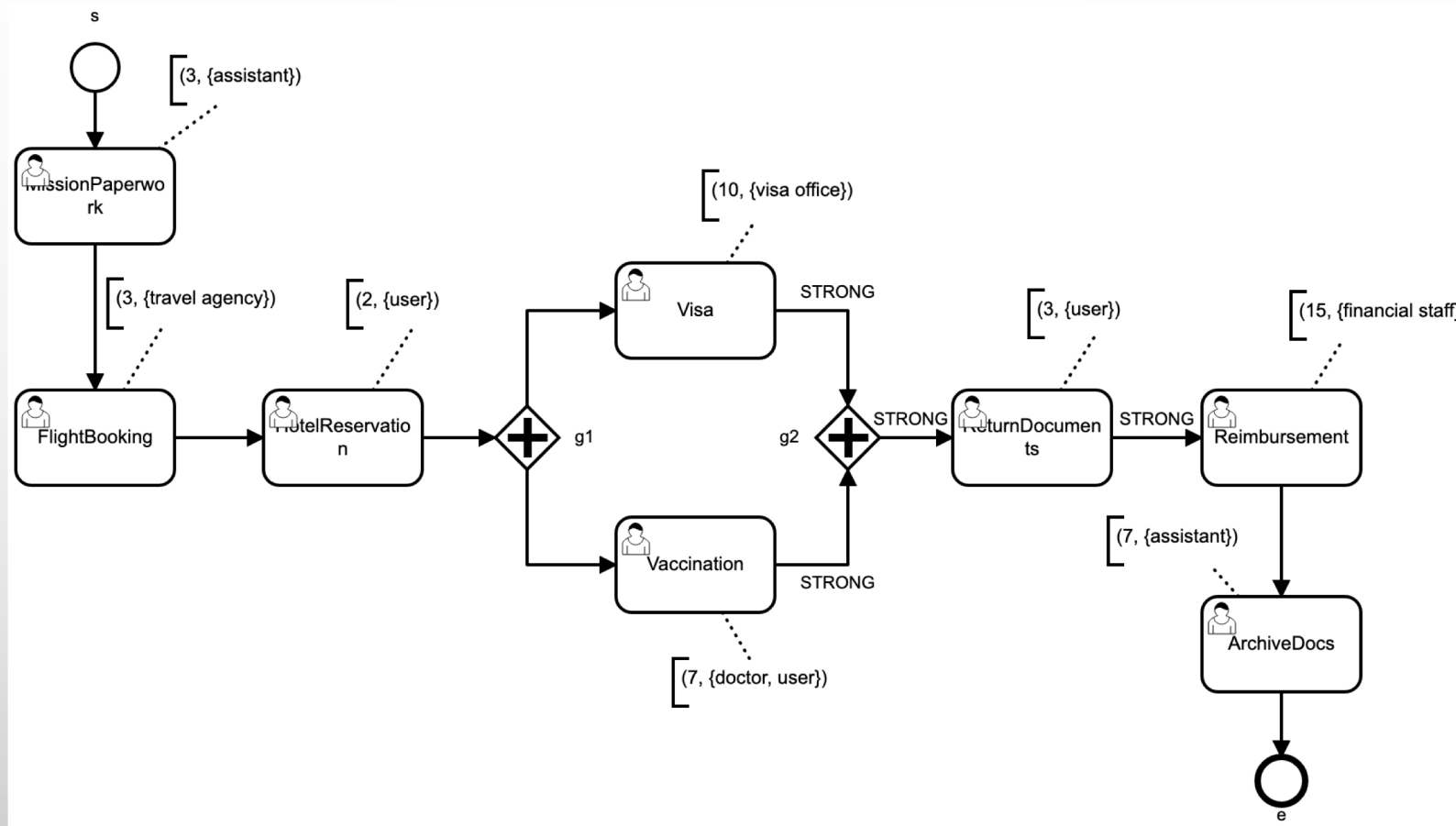
- MERGE EXCLUSIVE GATEWAY WITH PRECEDING TASKS (T1 SHARES RESOURCES WITH T, T2 DOES NOT SHARE RESOURCES WITH T)



- **MORE PATTERNS:** CASCADING MERGES, SPLIT PARALLEL GATEWAY, SPLIT EXCLUSIVE GATEWAY, ...

EXAMPLE: INITIAL PROCESS

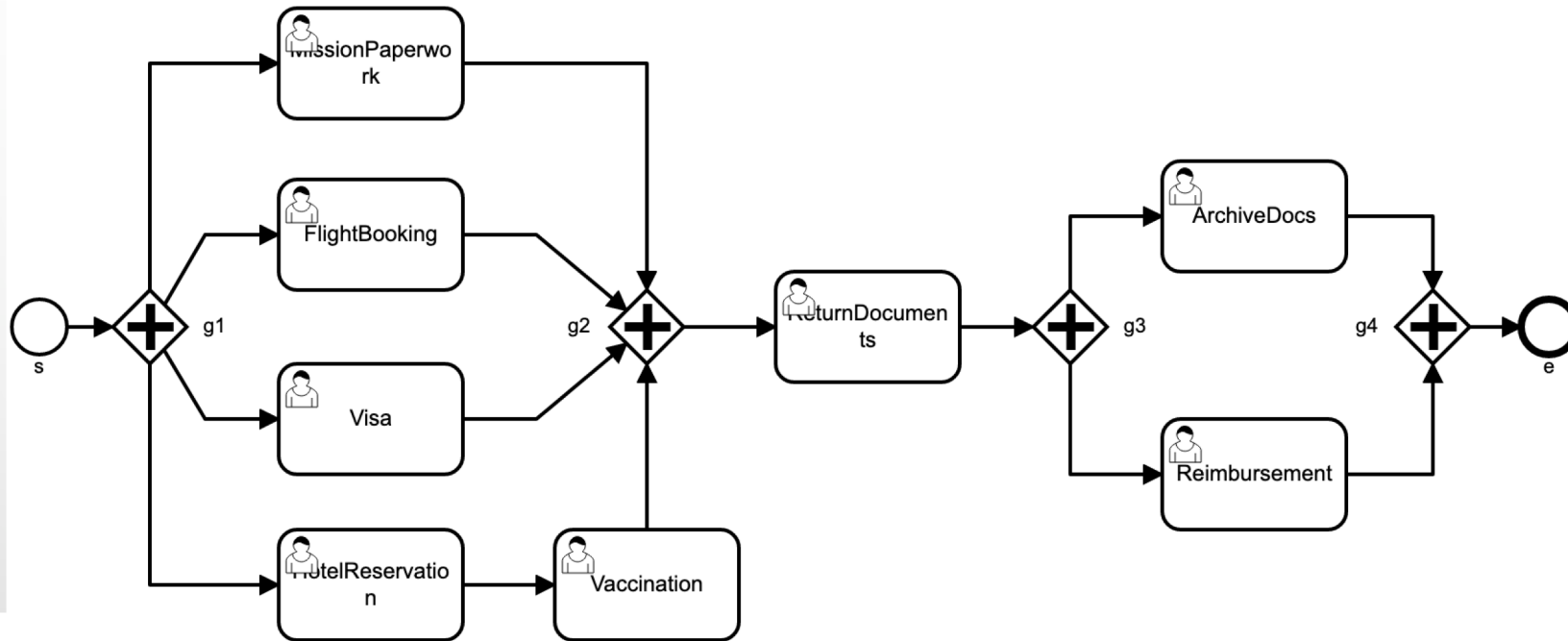
TRIP ORGANIZATION PROCESS



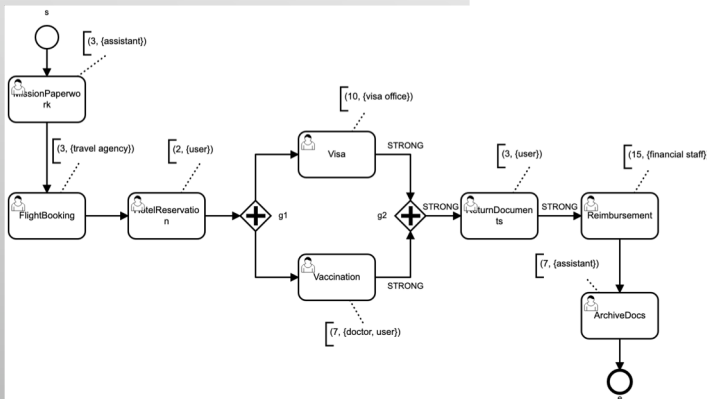
EXECUTION TIME:
43 DAYS

EXAMPLE: REFACTORED PROCESS












TRIP ORGANIZATION PROCESS



EXECUTION TIME:
28 DAYS



EXPERIMENTS

BPMN Proc.	Characteristics						Bounded Explo.		Heuristic	
	Tasks	Flows	Gateways	SF	AET _c	AET _b	AET	Time	AET	Time
1	5	13	4 	0	70	50	50	1s	50	1s
2	5	15	6 	0	40	25	25	2s	25	2s
3	6	13	2  2 	0	19	6	6	2s	9	1s
4	8	12	2 	4	43	28	28	21s	35	1s
5	8	12	2 	2	21	14	14	23s	16	1s
6	9	10	0	6	90	50	50	31s	90	1s
7	10	20	6 	0	24	18	19	38s	20	1s
8	10	20	2  4 	3	23	13	13	67s	17	1s
9	12	29	8 	0	200	120	140	50s	120	1s
10	15	36	10 	0	260	180	220	103s	260	3s

OUTLINE

1. BPMN WITH TIME AND RESOURCES
2. DESIGN TIME ANALYSIS
3. RUNTIME ANALYSIS
4. AUTOMATED REFACTORING
5. TOOL SUPPORT
6. CONCLUDING REMARKS

TOOL SUPPORT

■ DESIGN TIME ANALYSIS

- ORIGINAL VERSION BASED ON THE MAUDE FRAMEWORK (~4,000 LOC)
- RECENT VERSION WRITTEN IN JAVA, SPRING BOOT, POSTGRESQL, JAVASCRIPT, REACTJS, NODE.JS (~10,000 LOC)

MoudE3


Voyance

■ RUNTIME ANALYSIS: EXTENSION OF THE ACTIVITI FRAMEWORK + JAVA CODE (~4,000 LOC)

 **Activiti**


Java

■ REFACTORIZING TOOL IMPLEMENTED IN PYTHON (~5,000 LOC) + USE OF VBPMN FOR TRANSFORMATION FROM PYTHON TO BPMN

 **python™**

OUTLINE

1. BPMN WITH TIME AND RESOURCES
2. DESIGN TIME ANALYSIS
3. RUNTIME ANALYSIS
4. AUTOMATED REFACTORING
5. TOOL SUPPORT
6. CONCLUDING REMARKS

CONCLUDING REMARKS

- SEVERAL SOLUTIONS HAVE BEEN PRESENTED FOR THE **OPTIMIZATION OF BPMN PROCESSES** WITH TIME AND RESOURCES
- THE FIRST ONE FOCUSES ON THE PROBLEM OF **ALLOCATION OF RESOURCES** AND EXPLORED TWO COMPLEMENTARY OPTIONS (DESIGN TIME VS RUNTIME)
 - **DESIGN TIME APPROACH** IS USEFUL **BEFORE DEPLOYMENT** BUT STATIC ALLOCATION OF RESOURCES IS NOT OPTIMAL FOR UNSTABLE WORKLOADS
 - **RUNTIME APPROACH** DYNAMICALLY **UPDATES THE NUMBER OF RESOURCES** BUT THIS IS NOT ALWAYS POSSIBLE (EMPLOYEES)
- **REFACTORIZING TECHNIQUES** CHANGE A PROCESS INTO A NEW ONE, WHOSE EXECUTION TIME IS LOWER THAN THE ORIGINAL ONE

PERSPECTIVES

- DESIGN TIME / RUNTIME APPROACHES: THE **MODEL OF RESOURCES** NEEDS TO BE MORE ACCURATE (E.G., AN EMPLOYEE NEEDS BREAKS AND HOLIDAYS, A RESOURCE CAN BE EMPTY, ETC.)
- RUNTIME APPROACH: DEVELOP NEW DYNAMIC RESOURCE **ALLOCATION STRATEGIES** BASED ON **AI PREDICTION ANALYTICS**
- REFACTORING TECHNIQUES: INVESTIGATE **OTHER STRATEGIES** TO COMPUTE FASTER THE OPTIMAL PROCESS
- **SYNTHESIS TECHNIQUES** TO GENERATE AN OPTIMAL VERSION OF A PROCESS

SELECTED PUBLICATIONS

FRANCISCO DURÁN, YLIÈS FALCONE, CAMILO ROCHA, GWEN SALAÜN, AHANG ZUO:
FROM STATIC TO DYNAMIC ANALYSIS AND ALLOCATION OF RESOURCES FOR BPMN PROCESSES.
WRLA 2022.

FRANCISCO DURÁN, CAMILO ROCHA, GWEN SALAÜN: *RESOURCE PROVISIONING STRATEGIES FOR BPMN PROCESSES: SPECIFICATION AND ANALYSIS USING MAUDE.* J. LOG. ALGEBRAIC METHODS PROGRAM. 123, 2021.

FRANCISCO DURÁN, CAMILO ROCHA, GWEN SALAÜN: *A REWRITING LOGIC APPROACH TO RESOURCE ALLOCATION ANALYSIS IN BUSINESS PROCESS MODELS.* SCI. COMPUT. PROGRAM. 183, 2019.